

MICROCOPY RESOLUTION TEST CHART



**Technical Document 1071** April 1987

The Segmented Waveguide Program for Long Wavelength Propagation Calculations

J. A. Ferguson F. P. Snyder

AD-A181





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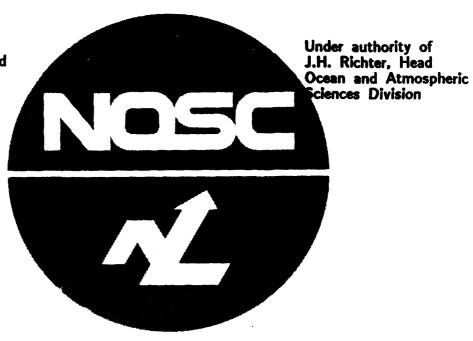
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## **ADMINISTRATIVE INFORMATION**

This work was performed by Code 544 of Naval Ocean Systems Center and funded by the Defense Nuclear Agency.

Released by J.A. Ferguson, Head Modeling Branch



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# UNCLASSIFIED SECURITY CLASSIFICATION OF THIS PAGE

# AD-A181939

REPORT DOCUMENTATION PAGE					
1a. REPORT SECURITY CLASSIFICATION	16. RESTRICTIVE MARKINGS				
UNCLASSIFIED					
28. SECURITY CLASSIFICATION AUTHORITY		3 DISTRIBUTION/AVAILABI	LITY OF REPORT		
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2b. DECLASSIFICATION/DOWNGRADING SCHEDULE					
4 PERFORMING ORGANIZATION REPORT NUMBER(S)	<del></del>	5 MONITORING ORGANIZAT	TION REPORT NUMBER(S	<del></del>	
NOSC TD 1071					
69 NAME OF PERFORMING ORGANIZATION	8b. OFFICE SYMBOL (if applicable)	7a NAME OF MONITORING ORGANIZATION			
Naval Ocean Systems Center	NOSC				
6c ADDRESS (City, State and ZIP Code)		76 ADDRESS (City, State and	d ZIP Code)		
San Diego, CA 92152-5000					
8a NAME OF FUNDING SPONSORING ORGANIZATION	8b. OFFICE SYMBOL (if applicable)	9 PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER			
Defense Nuclear Agency	DNA				
8c ADDRESS (City, State and ZIP Code)	· 1	10 SOURCE OF FUNDING N	UMBERS		
		PROGRAM ELEMENT NO	PROJECT NO	TASK NO	AGENCY ACCESSION NO
Washington, DC 20305		62715H	MP20		DN651 524
11 TITLE (include Security Classification)			<u> </u>		
The Segmented Waveguide Program for	Long Wavelength Propa	gation Calculation	8		}
12 PERSONAL AUTHOR(S)			<del></del>		
J.A. Ferguson and F.P. Snyder					
13a TYPE OF REPORT 13b TIME COV		14 DATE OF REPORT (Year,	Month, Day)	15 PAGE COUN	iT
Interim FROM	n 1986 to Dec 1986	April 1987 79			19
16 SUPPLEMENTARY NOTATION			•		
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	Longwave propagat		HITY DY DIOCK NUMBER)		· ·
FIELD GROUP SUB-GROUP	wavelength mode				
	propagation path,	V			
19 ABSTRACT (Continue on reverse if necessary and identify by block	number)				
A computer program which obtains	waveguide mode solutio	ns for very low fr	equencies and l	ow frequencies	(VLF/LF) is
described. The program allows for multiple homogeneous segments to be specified, allowing for consideration of variations					
in the earth-ionosphere waveguide. Path geometry and geophysical parameters can be computed by the program. Ionospheric disturbances due to man-made or naturally occurring events can also be modeled using the program.					
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UNCLASSIFIED UNLIMITED SAME AS APT DTIC USERS UNCLASSIFIED					
220 NAME OF RESPONSIBLE INDIVIDUAL		22b TELEPHONE (include A	Tree Code/	22c OFFICE SYMBOL	
J.A. Ferguson	(619) 225-2974		Code 544		

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# **CONTENTS**

Introduction	1
Program Control	2
Calculation of Mode Parameters	4
Path Calculations	8
Path Geometry	8 8 9
Presegmentation	ā
Mode Tracing	10
	11
Output	
Sample Input	12 14
References	14
APPENDIX	
Listing of the program	A-1
FIGURES	
rigures	
1. Canada Janua vaina COORD analan	40
1. Sample Input using COORD option	12
2. Sample input using PRESEG option	13
TABLES	
1. Summary of Control Strings	2
2. NAMELIST Inputs	4



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#### INTRODUCTION

The model of longwave propagation developed at the Naval Ocean Systems Center (NOSC) is based on a waveguide mode formulation. To determine signal levels in this approach the basic problem is to obtain the modal solutions to the specific waveguide under consideration (Pappert et al., 1970, Morfitt and Shellman, 1976), where complicated propagation paths are divided into horizontally homogeneous segments. The parameters of the segments are determined by the earth's ground conductivity, the magnitude and orientation of the geomagnetic field with respect to the direction of propagation, and the state of the ionosphere. Well-known computer programs which make the necessary calculations for a single set of propagation parameters are "WAVEGUID" (Pappert et al., 1970) and "MODESRCH" (Morfitt and Shellman, 1976). The WAVEGUID computer program and related programs are described in a series of reports and familiarity with the important elements of this series is assumed (Pappert. Gossard and Rothmuller, 1967; Sheddy et al., 1968; Pappert, Moler and Shockey, 1970; Morfitt and Shellman, 1976). This report describes a modified version of that program designed to supply calculations of long wavelength propagation along segmented propagation paths. This program is called the Segmented Waveguide (SW).

The computer program obtains waveguide mode solutions for very low frequencies and low frequencies (VLF/LF). The program allows for multiple homogeneous segments to be specified, allowing for consideration of variations in the earth-ionosphere waveguide. Path geometry and geophysical parameters can be computed by the program. lonospheric disturbances due to man-made or naturally occurring events can also be modeled using the program.

# Essential features of this program include:

- Automatic segmentation of the propagation path
- Allowance for presegmentation of the propagation path
- Allowance for variation of the ionosphere along that path

The program operates on propagation paths defined by a transmitter location and either a direction or a receiver location. A propagation path is defined as the great circle on a spherical earth. Variation of the geophysical parameters are to be expected along realistic paths. The diurnal condition in large part determines the significance of the other parameters. For instance, under daytime conditions the effect of variation of the geomagnetic field along a path is usually not significant to the resulting mode parameters. The program incorporates routines for calculating the parameters of the geomagnetic field and for selecting the ground conductivity at any point on the earth's surface.

Each of the path segments is treated as a horizontally homogeneous planar waveguide. Earth curvature is introduced by use of a modified refractive index. A set of possible solutions to the waveguide mode equation must be input. Each of these solutions is processed by an iteration routine. Each iteration requires computation of ionospheric and ground reflection coefficients. Calculation of the ionospheric reflection coefficients requires integration of the coefficients through the ionosphere. As approximate formulation may be used which requires a secondary set of complex angles be specified by the user. In that case, the ionospheric reflection coefficients are calculated for the secondary set of angles. These coefficients are used to interpolate the ionospheric reflection coefficients during the iteration of the primary set of possible solutions. This interpolation procedure requires much less computation time than does the more exact procedure.

The set of solutions for the first homogeneous segment must be input by the user. The program uses the results of up to three consecutive segments to extrapolate the solutions for successive segments. This reduces the number of iterations which are required for subsequent segments and allows for the tracing of mode solutions through a wide range of path variations.

The primary output of "SW" is data which may be used in mode summing programs. The strength of the electromagnetic field along the path can be obtained with either of two mode conversion models, one denoted "FULLMC" (Pappert and Shockey, 1972) and the other denoted "FASTMC" (Ferguson and Snyder, 1980). "FULLMC" does integrations through the ionosphere prior to calculating mode conversion coefficients and can be quite slow in execution time whereas "FASTMC" avoids the transionospheric integrations by use of approximations and runs quite quickly.

#### PROGRAM CONTROL

Program execution is controlled by strings containing mnemonic words. These strings and the sequence of operations initiated by them are described below. These control strings, as well as variable names and names of subroutines, appear in upper case. For clarity, the control strings are enclosed in single quotes and names of subroutines are enclosed in double quotes. Table 1 summarizes these control strings.

Table 1. Summary of control strings.

ID	run identification
NAME	general NAMELIST data
EIGEN	alternate EIGEN list input
PROFILE i	ionospheric specie profiles (i is 1 or 3)
COLFREQ	ionospheric collision frequency profiles
COORD	automatic segmentation of propagation path
PRESEG	presegmentated propagation path
QUIT	end of job

'ID' indicates that the next line of data to be read is a general identification for the path under consideration. This identification appears in the printout. It is also written to the mode parameter output file.

'NAME' initiates the reading of general program data via the NAMELIST: DATUM. Table 2 lists all variables, their type (I indicates integers, R indicates real (floating point) variables, C indicates complex variables), their units where applicable, and their initial values. If a variable defines an array, then the dimension of the array follows the name in parentheses. The NAMELIST input format is quite flexible but requires that column 1 be blank. Variable names are followed by an equal sign and then by the value of the variable. Array variable names may be followed by a string of values separated by commas and/or spaces. Embedded blanks are not allowed in the variable names. Variable types must be considered; for example, values for integer variables may not contain decimal points, but values for real variables do not have to have decimal points. Logical variables may be specified with any of '.true.' '.t.' 'f'. false.' '.f.' 'f'. The values of character variables must be enclosed within quotes. The first record of the NAMELIST input must contain '&name ' where 'name' is the

NAMELIST name (in this case, DATUM). The end of the NAMELIST is indicated by '&end'. Some of the values to be found in the following text are of the form A(N) to indicate A to the power N.

'EIGEN' allows for input of the list of trial solutions to be made from a file. The format of the input is the same as with NAMELIST. The control string is followed by the name of the file (starting in column 9) containing the NAMELIST data. The source of these input solutions could be a previous run with the program or from one of the automatic mode searching programs such as the one described by Morfitt and Shellman (1976).

'PROFILE i' initiates reading of the ionospheric charged particle profile data used to model the upper boundary of the earth-ionosphere waveguide. The value of i indicates the number of ionosperic species to be used and it must have one of two possible values: 1 is for electrons only and 3 is for electrons and ions. If i is not specified, a value of 1 is assumed. The use of i is shown below. The 'PROFILE i' string is immediately followed by a single line of identification for the profile. profile is input starting at the top of the ionosphere using a formatted input. Each line contains the height in km, the electron density at that height in electrons per cubic centimeter, and if ions are to be considered, the positive ion density at that height in ions per cubic centimeter. The height is in columns 1-7 and the electron and ion densities are required to be in columns 14-21 and 24-31, respectively. end of the profile is indicated by a dummy height with value less than zero. A maximum of 50 heights may be used. If i is 1, then only the electron density is read. Consequently, only the electron density need be present in the data. If i is 3, then the electron and positive ion densities are read and the negative ion density is computed by subtracting the electron density from the positive ion density (to preserve charge neutrality).

In the integration of the reflection elements through the ionosphere the program interpolates exponentially between input heights. The profile should contain sufficient data to define the ionospheric structure with height. For example, an exponential profile should consist of only the top and bottom heights and densities. Many regularly spaced heights tend to slow the integration.

A purely exponential conductivity profile (electrons only) may be input via the NAMELIST variables BETA and HPRIME.

Additional specie parameters are needed for the waveguide mode computations and are described below.

'COLFREQ' initiates reading of an ionospheric collision frequency profile. This allows use of nonexponential collision frequencies. The 'COLFREQ' string is immediately followed by the collision frequency profile, starting with the highest height and ending with a dummy height of value less than zero as in the case of specie profile described above. These heights need not match those used under 'PROFILE i'. The format of the data is the same as used for 'PROFILE i' except that collision frequency cannot be simply computed from the other two. If only electrons are being used, then only that collision frequency need be present. As with the specie profiles, the program interpolates exponentially between input heights.

An exponential collision frequency specification may be input via the NAMELIST variables EXPNU and COEFNU.

'COORD' initiates automatic segmentation of the propagation path. This string must be placed after all pertinent data have been read. This option is best applied to simple cases such as all daytime. The basic input consists of the path specification, the environment, and the starting mode solutions.

'PRESEG' allows for previously determined segments to be used along the propagation path. This option requires most of the same inputs as 'COORD' except that the user supplies the distances at which segments begin. At each segment the user has the option of specifying the parameters of the geomagnetic field, the ground and the ionosphere.

# **CALCULATION OF MODE PARAMETERS**

The inputs to the mode equation computations are supplied by geophysical routines and/or by the user. The subroutine which controls the calculations is "WVGUID". Most user supplied data values are input to the program via NAMELIST. These parameters are summarized in table 2 and are discussed in more detail below. In table 2 the data types are Integer (I), Real (R), and Complex (C).

Table 2. NAMELIST Inputs.

Varible	Туре	Default	Description
FREQ	R	0.0	Frequency in kHz Distance from the transmitter of the current segment in Mm.
RHO	R	0.0	
AZIM	R	0.0	Magnetic azimuth angle in degrees east of magnetic north.
CODIP MAGFLD	R R	0.0	Magnetic co-dip angle in degrees. Intensity of the geomagnetic field in Webers/square meter.
SIGMA	R	4.64	Ground conductivity in Siemens/meter.  Dielectric constant of the ground.
EPSR	R	81.0	
BETA	R	0.0	Slope of the exponential profile in km(-1) Reference height of the exponential profile in km.
HPRIME	R	0.0	
TLONG,TLA	R	0.0,0.0	Transmitter coordinates in degrees
RBEAR		720.0	Geographic bearing of the path in degrees
RLONG,RLA		0.0,0.0	Receiver coordinates in degrees
DRMIN	R	0.125	Minimum distance step size in Mm
DRMAX	R	0.5	Maximum distance step size in Mm
DMAX	R	20.0	Maximum distance in Mm
YEAR MONTH DAY GMT	I I R	0 0 0 0.0	Year Month number with January being 1 Day of the month Greenwich meridian time in hours
NPRINT NPROF	1	1	Flag used to control the amount of print out Flag to indicate which form of the profile is to be used

MIDPNT	1	0	Flag to indicate that only the midpoint is to be
IGCD	1	0	Flag to indicate that the computed distance between
IGND	ı	0	the transmitter and receiver is to be used Flag to indicate that the ground conductivity is to be
MDIR	1	0	determined from the ground map Flag used to reverse the direction of the magnetic field
EIGEN(60) TLIST(30)	C C	0.0,0.0 0.0,0.0	Initial solutions for the waveguide modes in degrees.  Angles where the reflection coefficients are computed for the inexact interpolation routine in degrees
DTHETA	C	0.01,0.001	Change in the mode solution used to define the
LUB	С	0.05,0.005	Tolerance used to test the differential change in the
DEIGEN FTOL	C R	0.05,0.005 1.0	mode solution. Used to stop the iteration  Tolerance used to define duplicate modes in degrees  Tolerance used to determine if the mode equation has been satisfied by the solutions
THTINC	R	0.5	Maximum change in degrees of either the real or imaginary part of the mode solution from one iteration to the next
MAXITR	I	7	Maximum number of iterations to attempt
ALPHA H	R R	3.14x10(-4) 50.0	The earth curvature correction factor in km(-1) Height at which the modified refractive index is unity in km
D	R	0.0	Height at which the integration through the ionosphere is stopped in km
PREC	R	2.0	Factor which controls the precision of the reflection coefficient integration
WR0	R	2.5x10(5)	Value of omega sub r used to define the reference
ATNMAX	R	50.0	height  Maximum attenuation rate of modes to be retained in dB/Mm
DEBUG	I	0	Flag used to generate additional printout for debugging purposes
TYPITR	1	0	Flag used to define the form of the mode equation
RPOLY NRTLST		1 5	Flag used to define the reflection coefficient calculation  Number of points to use in the interpolation of the
MKILSI	•	<b>3</b>	reflection coefficients during inexact iterations
LUNIT7	1	7	Logical unit number to which the mode parameters data are output
CHARGE(3)	R	-1.0, 1.0,-1.0	Charge of the ionospheric species
MRATIO(3)	R	1.0, 2*5.8x10(4)	Ratio of the mass of the ionospheric species to that of electrons
COEFNU(3)	R		Collision frequency of the ionospheric species at the ground in collisions/sec
EXPNU(3)	R		Exponential slope of the collision frequency in km(-1)

The radio frequency in kHz is specified by the variable FREQ. The input to subroutine "WVGUID" includes an ionospheric profile. The variable NPROF controls which ionospheric profile is to be used. A value of 0 indicates that the profile input via 'PROFILE i' is to be used. A value of 1 indicates that an exponential electrons only profile is to be used. The profile is specified by the exponential slope BETA in km(-1) and a reference height HPRIME in km (Wait and Spies, 1964). A value of 2 for NPROF is used to indicate that a series of profiles will be input. This option only applies to 'PRESEG'. The profiles are to be input using the same format as described under 'PROFILE i', including the control string. There must be a profile for each segment.

Additional specie parameters are needed. The number and order of these specie parameters must be consistent with the charged particle densities of 'PROFILE i'. The charges of the species are input as CHARGE (i.e., CHARGE = -1, +1, -1). The masses of the species relative to that of an electron are input as MRATIO. The collision frequencies may be defined with 'COLFREQ' (nonexponential) or with the variables COEFNU in collisions per second and EXPNU in km(-1). The collision frequency v at an altitude z is then defined by

v = COEFNU \* exp(EXPNU \* z)

where z is in km.

Parameters of the geomagnetic field are specified by AZIM, the angle between magnetic north and the direction of propagation in the horizontal plane measured in degrees east of north, CODIP, the magnetic co-dip angle measured from the vertical (i.e., the north pole has a CODIP of 0), and MAGFLD, the magnetic intensity in Webers per square meter or in Gauss. The magnitude of MAGFLD is tested. If it is greater than 10(-2) then the input value is assumed to be in Gauss and is multiplied by 10(-4).

MDIR is a flag that when set to 1, causes the direction of propagation as input to be reversed. This allows for development of a data set appropriate to examining transmitter deployment.

Ground conditions are specified by SIGMA, the conductivity in Siemens/m, and EPSR, the relative dielectric constant.

The presegmentation option allows the magnetic field and ground parameters to be varied by the user.

The correction for earth curvature is controlled by ALPHA in km(-1) which is defined as 2 over the radius of the earth. For a curved earth ALPHA is 3.14x10(-4) km(-1) and for a flat earth ALPHA is 0.

lonospheric altitude parameters are H, which is the height in km at which the modified refractive index is unity and is the height to which the mode solutions are referenced; D, which is the height in km below which ionospheric effects can be ignored. D must be equal to or greater than the bottom height of the ionospheric profiles used. It is usually sufficient to choose H equal to D. The choice of D and H is also discussed by Pappert et al. (1967).

The trial eigenangles follow the variable name EIGEN which is a complex variable. Up to 60 eigen angles may be input. If little is known about the expected solutions for a given set of conditions, a set of approximate solutions may be obtained using a TLIST. The TLIST is a list of as many as 30 complex angles which are used to set up an interpolation matrix of the ionospheric reflection elements (Sheddy et al., 1968) The program then uses this matrix to interpolate reflection elements during the iterative process used to obtain mode solutions. These solutions are referred to as "inexacts" in order to distinguish them from the more accurate solutions using integrated reflection coefficients. The variable NRTLST determines the maximum number of TLIST angles used in each interpolation. During the inexact iteration process, the program computes the magnitude of the complex difference between the current value of the solution and each of the TLIST angles. The program orders the TLIST angles from the product to the largest difference and selects the first NRTLST of them to be used in the interpolation. This improves the accuracy of the interpolated reflection coefficients and reduces the number of terms used.

If more than 30 EIGENs are input, then the program sorts the angles according to their attenuation rate and deletes those with attenuation rates greater than a user specified maximum. The initial value of this maximum is ATNMAX. If there are still more than 30 angles, then the maximum attenuation rate is reduced by 5 dB/Mm and the input list is sorted again. This process is repeated until there are less than 30 angles in the list.

If the number of EIGEN or TLIST inputs varies from one NAMELIST to the next, then each EIGEN or TLIST list should be terminated with a zero. If RPGLY is not 0 and the first value of TLIST is 0, then TLIST is set equal to the first 30 EIGENs.

The Newton-Raphson iteration process, used to find the eigenangles which sales the modal equation is described by Sheddy et al. (1968). Iteration is performed for each input EIGEN. The iteration stops when the maximum number of iterations (MAXITR) is exceeded or when the change in the real and imaginary parts of the solution is calculated to be less than the real and imaginary parts of LUB, respectively.

The type of solution obtained is determined, in part, by RPOLY, which can have three values: 0 for exact solutions only, 2 for inexact (approximate) solutions only, and 1 for inexacts computed and used as inputs to obtain exact solutions. The use of RPOLY equal to 1 is described more fully below.

The flag TYPITR is used to obtain vertically polarized modes only (TYPITR equal to 1) or horizontally polarized modes only (TYPITR equal to 2). It is physically meaningful to apply this option only for nearly isotropic conditions, no magnetic field (MAGFLD set to 0), or east to west and west to east propagation at the geomagnetic equator (CODIP is 90 and AZIM is 90 or CODIP is 90 and AZIM is 270).

To ensure consistent mode sums and eliminate redundant solutions, each exact and inexact EIGEN solution is tested for several conditions. The first is that the imaginary part of the solution must be less than zero in order to have attenuating modes. The second is that the magnitude of the modal equation must be less than FIOL. This parameter is tested only for final solutions and only if the number of iterations required to obtain the solution is greater than or equal to MAXITR. It is generally true that if the iteration stops because the change in the mode solution is less than LUB, then the value of the mode equation is small. There are instances in which the test on FTOL will still fail. Consequently, the value of FTOL is set very high in order to allow the

program to continue execution. In some cases the user may want to modify the default value in order to perform special tests. If RPOLY is 1, the inexacts are treated as intermediate results. The third test is that the value of the EIGEN solution must be different from all previous solutions by an amount DEIGEN which is input as a complex number. The real and imaginary parts of DEIGEN are the tolerances for the real and imaginary parts of the EIGEN solutions, respectively. If one of the above tests results in a mode being dropped from the list of solutions, then the program follows the procedures outlined below under the discussion of mode tracing.

Subroutine "WVGUID" computes and prints attenuation rate in dB/Mm, phase velocity relative to the speed of light, the magnitude, and phase of Wait's excitation factor (Wait, 1962) at the ground in dB and radians.

The headings for the number of iterations to go from the input angle to the final solution, the final solution, the magnitude of the modal equation, and the magnitude of the polarization mixing ratio are printed as ITER, EIGEN, MAG F, and MAG P, respectively. The attenuation rate, phase velocity relative to the speed of light, magnitude, and phase of Wait's excitation factor, and the final solution references to the ground are printed under the headings of ATTEN, V/C, WAIT'S EXC, and THETA', respectively.

The parameters YEAR, MONTH, DAY, and GMT are used only to pass the values to the output files. These parameters are useful for helping to identify the output data to programs which may use this information.

## PATH CALCULATIONS

These calculations are controlled by "GCPATH". They can be divided into three classes. The first automatically computes geometry and geophysical parameters which are obtainable from just the location of a point on the propagation path or uses presegmented distances and geophysical parameters. In addition, the program extrapolates the EIGEN list and TLIST so as to trace modes along a path.

#### PATH GEOMETRY

All geometry calculations are for a spherical earth. Inputs to this portion of the program consist of transmitter and receiver locations, path length, and path increments. Transmitter and receiver longitude and latitude are input with TLONG and RLONG and TLAT and RLAT. The convention used in the program is east longitude and south latitude are negative. An alternate input for the receiver position is its bearing, RBEAR, in degrees east of north. In the execution of the program RBEAR is tested. If RBEAR is 720, then the program uses RLONG and RLAT to define the path. If RBEAR is not 720, then it and the input path length, DMAX, are used to define the path. DMAX is specified in megameters and must be less than or equal to 20. If RLONG and RLAT are used, there are two path lengths possible. If the parameter IGCD is equal to 1, the path length is set equal to the computed short great circle distance between the transmitter and receiver. If IGCD is equal to 0, the path length is unchanged from what was input (DMAX). If the path bearing is input, the path length is always DMAX.

The starting value of the distance from the transmitter is input as RHO and is in Mm. The path increments are controlled by the mode tracing results and the variables DRMIN and DRMAX which are all in units of Mm. The procedures of the values are described as follows.

The geomagnetic field is computed at the first path point defined by Kill and at the beginning of each path segment. The ground conductivity and relative dielectric constant are specified by the user through SIGMA and EPSR via NAMELIST or by searching the ground map. If IGND is 0, the ground map is not searched and ground conditions are assumed constant, as input, for the entire path for 'COORD' or as varied by the user for 'PRESEG'. If IGND is 1, the DECO-NRL 10 level ground conductivity map (Hauser, Garner, and Rhoads, 1969) is searched for the appropriate values of SIGMA and EPSR at the beginning of each path segment.

If the value is assumed that the entire propagation path can be described adequately by the conditions at the midpoint of the path, then the path conditions at that point can be obtained if MIDPNT is set to 1. The subsequent modal calculations will then be for the midpoint conditions.

At the transmitter and at the end of each path segment, the parameters to be used in the "WVGUID" calculations are printed next to the heading, PROPAGATION PATH PARAMETERS, as described below. In addition, the distance in megameters from the transmitter, the coordinates and the geographic bearing of the path at the current point are printed under the headings RHO, LAT, and BEAR, respectively. If the midpoint option is being used, then the above information for the midpoint is printed.

#### **PRESEGMENTATION**

In some instances, user segmentation of the propagation path is desired. The control string 'PRESEG' allows arbitrary segmentation of the path. This is accomplished by a succession of data lines in list directed format containing values for path distance in Mm, AZIM, CODIP, MAGFLD, SIGMA, EPSR, BETA, and HPRIME, respectively. List directed input is accomplished by entering values separated by commas or spaces. There must a data entry for each request in the input list. If a value is not to change from one data line to the next, then the value need not be entered but its omission must be indicated by a pair of commas. The first value of path distance need not be zero. The presegmentation is terminated by a distance value of 40.

If NPROF is 0, the ionospheric profile is constant for the path and is defined by 'PROFILE i'. If NPROF is 1, then the values of BETA and HPRIME on the presegmentation data lines are examined. If BETA is zero, then the previously defined values of BETA and HPRIME are used. The latter may be input via NAMELIST so that a constant ionosphere for the path can be obtained by using NAMELIST input. If either of the values of BETA and HPRIME are to change, both must be input. If NPROF is 2, then each presegmentation data line must have a corresponding 'PROFILE i' profile specification on logical unit 3.

The following conventions are used for using the values of the presegmentation data. If the value of MAGFLD is zero or blank, then the magnetic field parameters are calculated. If a nonzero value is specified, then all of the magnetic field parameters are taken from the presegmentation data. If constant magnetic pair netwice are desired along the path, the values must be specified on each presegmentation data line. If the value of SIGMA is not entered, then the previously specified value of SIGMA and EPSR are used. Otherwise, the values of these parameters are taken from the presegmentation data line. Constant values for the whole path may be specified via NAMELIST or in the first presegmentation card. If IGND is 1, then the ground

map is searched and the values of SIGMA and EPSR on the cards are ignored. If BETA is not entered, the currently defined values are used for the electron density profile. Even if only one value in the pairs SIGMA, EPSR, and BETA, HPRIME is to be changed, both values must be specified.

### MODE TRACING

Efficient computation of mode parameters along the propagation path is best achieved by using RPOLY set to 1, which will be assumed for the rest of this discussion. At the first point on the path, solutions are best obtained by using a TLIST composed of angles which are believed to be approximately correct and an EIGEN list of many regularly spaced angles such as 88, -1, 87, -1, 86, -1, etc. Alternatively, the EIGEN list should be the list of approximately correct solutions with the TLIST set to zero or the 'EIGEN' control string could be used to specify solutions from some other source. The program computes inexact solutions for the conditions at the first point on the path. After exhausting the EIGEN list, obtaining inexact solutions, and deleting of those failing the tests discussed above, exact solutions are computed using the results of the inexacts.

Now the discussion must be separated for the two-path segmentation options. For the 'COORD' option, the second point on the path is DRMIN from the transmitter. For this point, the final solutions for the first point are placed in both TLIST and EIGEN and the same process of calculation of inexacts and exacts is repeated. If DRMIN is not too far from the transmitter and/or the geophysical parameters do not change too much, then this step in the extrapolation process is quite efficient. Now the program has two sets of final solutions and makes a linear extrapolation for TLIST and EIGEN angles for the third point on the path which is twice DRMIN from the transmitter. The sequence of calculations for the inexact and exact solutions is repeated. For the fourth and all subsequent points on the propagation path, the program uses the previous sets of final solutions to make second order extrapolations for TLIST and EIGEN angles. The distance increments are chosen as described below.

As the program steps out along the propagation path, modal solutions may be lost or removed. First, a mode may be lost in the screening process in subroutine "WVGUID" as described above. At the first point on the path, modes may be overlooked simply because of lack of adequate trial solutions and/or more than one EIGEN input resulting in the same final solution, perhaps due to closely spaced input EIGEN values. If computations are being made at the transmitter or at the midpoint, it is acceptable to lose a solution from the input EIGEN list. At all other points, when a mode is lost execution terminates in "WVGUID". After the tests on the solutions in "WVGUID" are completed at the first point on the path, the program assumes that it has a complete set of modes. After this set is established, solutions may be acceptably removed only in the extrapolation subroutine, "EXTRAP". The solutions produced by "WVGUID" for the current segment are used to compute attenuation rates. Those solutions whose attenuation rate exceeds ATNMAX are deleted from the list. The location of the solution in the set is marked and its removal is indicated by a blank line in the printout of solutions produced by subsequent "WVGUID" calculations.

If a mode is lost during "WVGUID" calculations, the path point is moved back to about halfway between the current point (where a solution was lost) and the previous point (where all solutions were obtained). The actual distance depends on the current value of the distance increment. If the increment is greater than DRMIN, then the

new increment is chosen that it is an integral multiple of DRMIN and is less than crequal to half the previous increment. Geophysical parameters at the new path point are computed, the EIGEN list is revised by "EXTRAP", and "WVGUID" calculations are repeated.

If no modes are lost and the number of iterations required to obtain the solutions is less than or equal to half of MAXITR, then the distance increment is increased by DRMIN. This increase in the distance increment can continue until the path increment is equal to DRMAX. If no modes are lost and the number of iterations required to obtain the solutions is greater than half of MAXITR, the path increment is decreased by DRMIN.

If modes are lost and the separation between the previous point (for which all modes were found) and the current point (for which modes were lost) is less than or equal to DRMIN, then the distance increment is halved. The geophysical parameters for the new path point are linearly interpolated using the parameters of the two points at which geophysical parameters were computed, the EIGEN list is revised by "EXTRAP", and "WVGUID" calculations are repeated. Solutions obtained for interpolated path points are not saved. They are used only to trace the mode solutions between the points for which the geophysical parameters are computed.

If no modes are lost and the number of iterations required to obtain the solutions is less than or equal to half of MAXITR, then the distance increment is doubled. This increase in the distance increment can continue until the path increment is equal to the distance to the end of the interpolation interval. If no modes are lost and the number of iterations required to obtain the solutions is greater than half of MAXITR, the path increment is halved. If the new distance increment is less than 15 km, then the program aborts.

For the 'PRESEG' option, the distance increment is controlled by the intervals between the presegmented distances. When modes are lost, the interpolation procedure for cases in which the backup interval is less than DRMIN described above is followed.

### OUTPUT

Mode parameters from the program are written to the logical unit whose numerical value is LUNIT7. The first line of data written contains the transmitter location, path bearing, and the date and time, as input through NAMELIST. The identification which followed 'ID' is written next. If no identification was specified with 'ID', this line of data is blank. The identification is followed by a sequence of lines at each output distance.

The first line of data at each such distance contains the distance, frequency, AZIM, CODIP, MAGFLD, SIGMA, EPSR, and the reference height of the ionospheric profile. In descriptions of other programs, this first line of data at each distance is referred to as the RFACMSET header. This header line is followed by pairs of data lines, one pair for each mode. The quantities in these data lines are the mode solution as a complex angle in degrees, a flag, T1, T2, T3, and T4. The parameters T1, T2, T3, and T4 are described in detail by Ferguson and Snyder (1980). The last line of data at each output distance is blank. These data are suitable for use in "FASTMC" (Ferguson and Snyder, 1980).

If the program fails because of some problem at the first path point, it writes 'Failure at RHO 1' to logical unit 90. Otherwise, it writes the distance of the last point for which "WVGUID" successfully completed. If the end of the path is reached, then this distance is output as 40.

### SAMPLE INPUT

Sample input files are shown in figures 1 and 2. In the first sample (figure 1), the path is to be run for all nighttime conditions assuming all seawater ground. The EIGEN list for the transmitter is input directly and the automatic path segmentation is to be used.

```
id
Sample run
name
&datum freq=23.4 h=50 d=75 lunit7=7 atnmax=50
tlong=150 tlat=20 rbear=10 dmax=10
lub=.005 .0005 dtheta=.01 .001
deigen=.05 .005 thtinc=.05
beta=.43 hprime=87
eigen= 85.678 -0.206 84.595 -0.688 81.806 -0.609 81.027 -0.255
77.653 -0.791 77.023 -0.269 73.199 -0.825 72.980 -0.300
68.926 -0.264 68.599 -0.955 64.751 -0.213 63.907 -1.144
60.457 -0.183
&end
coord
```

Figure 1. Sample input using COORD option.

The second example (figure 2) is a much more complicated case. It is for the same path of the first sample, but the ionosphere is to be varied according to the diurnal conditions along the path for July 15 at 1612Z. The transition from night to day has been modeled as five steps starting with BETA at 0.30 and HPRIME at 74 and ending with BETA at 0.43 and HPRIME at 87. In addition, the ground conductivity for the last profile takes on three values: 4, 10(-2), and 10(-3). In order to improve the efficiency of the mode tracing, additional segmentation has been performed so that each ground conductivity is processed separately. The segmentation does not produce final output that is monotonically increasing in distance from the transmitter. The necessary ordering of the segments must be performed by editing the final output file or by a user supplied program. The initial mode solutions for each segment have been already calculated and stored in a set of files named XMTR202.MFx where x ranges from 0 to 6.

```
Sample run
name
 &datum freq=23.400 h=50. lunit7=7 atnmax=50.
 lub=0.005 0.0005 dtheta=0.010 0.0010
 deigen=0.050 0.0050 thtinc=0.05
 year=84 month= 7 day=15 gmt=16.2
 tiong= 158.150 tlat= 21.417 dmax=4
 rbear=202.0 &end
eigen xmtr202.mf0
preseg
 0.000,190.6, 50.8,0.350,4.E+00,81.,0.30,74.0,
40,0,0,0,0,0,0,0,0,
eigen xmtr202.mf1
preseg
 0.500.190.8. 56.8.0.337.4.E+00.81..0.32.76.2.
40,0,0,0,0,0,0,0,0
eigen xmtr202.mf2
preseg
 0.960,190.9, 63.1,0.329,4.E+00,81.,0.34,78.3,
40,0,0,0,0,0,0,0,
eigen xmtr202.mf3
preseg
 1.040,190.9, 64.2,0.327,4.E+00,81.,0.37,80.5,
 1.240,190.9, 67.3,0.325,4.E+00,81.,0.37,80.5,
40.0.0.0.0.0.0.0.
eigen xmtr202.mf4
preseg
 1.340,190.9, 68.8,0.324,4.E+00,81.,0.39,82.7,
 1.540,190.9, 72.1,0.323,4.E+00,81.,0.39,82.7,
40,0,0,0,0,0,0,0,
eigen xmtr202.mf5
preseg
 1.640,190.9, 73.8,0.322,4.E+00,81.,0.41,84.8,
 1.820.190.9. 76.8.0.322.4.E+00.81..0.41.84.8.
40.0.0.0.0.0.0.0.
eigen xmtr202.mf6
preseg
 1.940,190.8, 78.9,0.322,4.E+00,81.,0.43,87.0,
 2.120,190.8, 82.2,0.323,4.E+00,81.,0.43,87.0,
 2.300,190.7, 85.5,0.324,4.E+00,81.,0.43,87.0,
 2.480,190.6, 88.8,0.326,4.E+00,81.,0.43,87.0,
 2.660,190.6, 92.1,0.329,4.E+00,81.,0.43,87.0,
 2.840,190.5, 95.5,0.333,4.E+00,81.,0.43,87.0,
 3.020,190.4, 98.9,0.337,4.E+00,81.,0.43,87.0,
40,0,0,0,0,0,0,0,0
```

Figure 2. Sample input using PRESEG option.

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- Pappert, R. A. and L. R. Shockey, "A Simplified Mode Conversion Program for VLF Propagation in the Earth-Ionosphere Waveguide", DASA Interim Report No. 751, October 1974.
- Sheddy, C. H., R. A. Pappert, Y. A. Gough, and W. F. Moler, "A FORTRAN Program for Mode Constants in an Earth-Ionosphere Waveguide", DASA Report 683, May 1968.
- Wait, J. R., Electromagnetic Waves in Stratified Media, Pergamon Press, New York, p. 221, 1962.

APPENDIX: LISTING OF THE PROGRAM

```
0001
        C
              SW:
                    SEGMENTED WAVEGUID
0002
        c
0003
               include 'common1.for/list'
0004
      1 c
0005
      1
              common/input/freq,rho,azim,codip,magfld,sigma,epsr,beta,hprime,
0006
      1
               common/path/pathid, tlong, tlat, rlong, rlat, rbear, dmax, drmin, drmax,
0007
      1
8000
                      year, month, day, gmt, nprint, nprof, npath, igcd, ignd, mdir, lost,
      1
0009
      1
                      lunit7,lx
               common/ionosp/htlist(50), Inlist(50,3), hclist(50), cflist(50,3),
0010 1
0011
                      charge(3), mratio(3), nrspec, lhtmx, lhtmn, lht, mhtmx, mhtmn, mht
0012
      1 c
0013
      1
               character + 80 pathid
0014
      1
               integer year,day
0015
               real *4 freq, rho, azim, codip, magfld, sigma, epsr, beta, hprime, hprout,
0016
      1
                      tlong, tlat, rlong, rlat, rbear, dmax, drmin, drmax, gmt,
0017
                      htlist, Inlist, hclist, cflist, charge, mratio
      1
0018 1 c
0019
               include 'common1.ini/list'
0020 1 c
0021 1 c
               initialize common1
0022
               data freq/0./,rho/0./,azim/0./,codip/0./,magfld/0./,
      1
0023
                    sigma/4.64/,epsr/81./,beta/0./,hprime/0./,
      1
0024
              $
      1
                    tlong/0./,tlat/0./,rlong/0./,rlat/0./,rbear/720./,
0025
              2
      1
                    dmax/20./,drmin/.125/,drmax/.5/,mdir/0/,
0026 1
                    year/0/,month/0/,day/0/,gmt/0./,nprint/1/,nprof/1/,
0027
                    igcd/0/, ignd/0/, mdir/0/, lunit7/7/,
                    charge/-1.,1.,-1./,mratio/1.,2*58000./,nrspec/1/
0028
      1
0029
     1 c
0030
               include 'common2.for/list'
0031
0032
               common/wg in/elist(2,30),tlist(2,30),dtheta(2),lub(2),deigen(2),
      1
0033
      1
                      thtinc, ftol, maxitr, alpha, h, d, prec, wrO, atnmax, debug, typitr,
0034
      1
                      rpoly, nrtlst
0035
               common/wg out/tp(30), tterm(4,30), nterm(30), mode(30), modes, nmds
     1
0036 1 c
0037 1
               complex*8 tp,tterm,dthta
0038
      1
               integer debug, typitr, rpoly
0039
               real+4 elist,tlist,dtheta,lub,deigen,thtinc,ftol,alpha,h,d,prec,
      1
0040
      1
                      wr0,atnmax
0041
      1 c
0042
               equivalence (dtheta, dthta)
      1
0043
      1 c
0044
               include 'common2.ini/list'
0045 1 c
0046
     1 c
               initialize common2
               data elist/60*0./,tlist/60*0./,
0047
      1
0048
                    dtheta/.01,.001/,lub/.05,.005/,deigen/.05,.005/,thtinc/.5/,
      1
0049
                    ftol/1000./,maxitr/7/,alpha/3.14e-4/,h/50./,d/0./,prec/2./,
      1
0050
                    wr0/2.5e5/,atnmax/50./,debug,typitr/0,0/,rpoly/1/,nrtlst/5/
      1
0051
      1 c
0052
        c
0053
               namelist/datum/freq,rho,azim,codip,magfld,sigma,epsr,beta,hprime,
0054
                        tlong, tlat, rlong, rlat, rbear, dmax, drmin, drmax,
0055
              $
                        year, month, day, gmt, nprint, nprof, midpnt, igcd, ignd, mdir,
0056
              $
                         lunit7, charge, mratio, coefnu, expnu,
              $
0057
                        eigen, tlist, dtheta, lub, deigen, thtinc, ftol, maxitr,
```

```
SWSMAIN
```

```
0058
             $
                        alpha, h, d, prec, wr0, atnmax, typitr, rpoly, nrtlst
0059
        С
0060
              complex theta
0061
              character* 8 branch
0062
              character + 40 fname
0063
               character *80 bcd
0064
        C
0065
              dimension coefnu(3), expnu(3), eigen(2,60)
0066
        C
0067
               Initialize MAIN
        С
0068
              data nuflag/0/,coefnu/1.816e11,2*4.540e09/,expnu/3*-.15/,
0069
                    eigen/120+0./,midpnt/0/
0070
        C
0071
              Unit:
                           Useage:
        C
0072
                   2
                                   input of alternate eigen list
        c
                                   input of profiles along the path
0073
                   3
        c
0074
                   lunit7
                                   output of mode parameters along the path
        С
0075
        С
0076
        c
               read(5,1000,end=999) bcd
0077
        10
0078
               print 1001,bcd
0079
               branch=bcd(1:8)
               if (branch .eq. 'id
0080
                                          .or. branch .eq. 'ID
                                                                      ') go to 20
0081
               if (branch .eq. 'name
                                          .or. branch .eq.
                                                            'NAME
                                                                      ') go to 100
0082
               if (branch .eq. 'eigen
                                          .or. branch .eq.
                                                            'EIGEN
                                                                      ') go to 130
               if (branch .eq. 'profile '
0083
                                          .or. branch .eq.
                                                            'PROFILE
                                                                     ') go to 200
               if(branch .eq. 'colfreq'
                                                            'COLFREQ ') go to 250
0084
                                          .or. branch .eq.
                                                                      ') go to 400
                                                            'PRESEG
0085
               if (branch .eq. 'preseg
                                          .or. branch .eq.
                                        '.or. branch .eq.
                                                                      ') go to 500
0086
               if (branch .eq. 'coord
                                                            'COORD
                                        ' .or. branch .eq. 'QUIT
                                                                      ') go to 999
0087
               if (branch .eq. 'quit
0088
        C
0089
               print *, 'ABORT MAIN: Control card not recognized '
0090
               stop
0091
        С
0092
        С
               Path identification
        20
0093
               read(5,1000) pathid
0094
               print 1001, pathid
0095
               go to 10
0096
        C
0097
               NAMELIST input
        100
0098
               read(5,datum)
0099
               if(nprint .gt. 1) print datum
0100
               if (freq .eq. 0.) then
                 print +, 'ABORT MAIN: FREQ not input '
0101
0102
                 stop
0103
               end if
0104
               if(magfld .gt. 1.e-02) magfld=magfld*1.e-04
0105
               go to 10
0106
        C
0107
              Separate EIGEN list input
        C
0108
        130
               read(bcd,1004) fname
0109
               open(unit=2, file=fname, status='old')
0110
               read(2,datum)
0111
              close(unit=2)
               if(nprint .gt. 1) then
0112
                 do 131 m=1,60
0113
0114
                 if (eigen(1,m) .eq. 0.) go to 132
```

#### SWSMAIN

```
0115
        131
                 km=m
        132
                 print 1040,d,h, (eigen(1,k),eigen(2,k),k=1,km)
0116
0117
               end if
0118
              go to 10
0119
        C
              Profile input
0120
        c
0121
        200
               read(bcd,1002) number
0122
               nrspec=maxO(1, number)
0123
               nprof=0
               call profin(5,1,50,nprint,nrspec,lhtmx,htlist,lnlist)
0124
0125
               if(lhtmx .le. 0) then
0126
                 print +, 'ABORT MAIN: Ionospheric profile missing'
0127
                 stop
0128
               end if
               go to 10
0129
0130
        C
0131
               Collision frequency profile input
        250
0132
               nuflag=1
0133
               call profin(5,2,50,nprint,nrspec,mhtmx,hclist,cflist)
0134
               if (mhtmx .le. 0) then
0135
                 print *, 'ABORT MAIN: Collision frequency profile missing'
0136
                 stop
0137
               end if
0138
               go to 10
0139
        C
0140
        c
               Presegmented path
0141
        400
               npath=2
0142
               go to 600
0143
        C
0144
               Automatic path segmentation
        С
0145
        500
               npath=midpnt
0146
        c
0147
               Test all inputs before execution.
        C
0148
        С
               Count the modes
0149
        С
0150
        600
               do 602 m=1,60
0151
               if(eigen(1,m) .eq. 0.) go to 603
        602
0152
               nmds=m
        603
0153
               if (nmds .le. 0) then
                 print *, 'ABORT MAIN: No EIGEN list '
0154
0155
                 stop
0156
               end if
0157
               Delete duplicate modes using DEIGEN
        C
0158
               if (nmds .gt. 1) then
0159
                 m=1
                 1=2
0160
        605
0161
                 if(abs(eigen(1,m)-eigen(1,l)) . It. deigen(1) . and .
0162
                    abs(eigen(2,m)-eigen(2,1)) . It. deigen(2) then
0163
                   Found a match so drop this mode.
        c
0164
                   do 607 k=1,nmds
0165
                   eigen(1,k)=eigen(1,k+1)
        607
0166
                   eigen(2,k)=eigen(2,k+1)
0167
                   eigen(1,nmds)=0.
0168
                   eigen(2,nmds)=0.
0169
                   nmds=nmds-1
0170
                   if(I .le. nmds) go to 605
0171
                 end if
```

```
SWSMAIN
```

```
0172
                 if(| .lt. nmds) then
0173
                   |=|+1
                   go to 605
0174
0175
                 end if
0176
                 if (m . lt. nmds) then
0177
                   m=m+1
0178
                   l=m+1
0179
                   go to 605
0180
                 end if
0181
               end if
0182
        C
0183
        610
               if (nmds .gt. 30) then
0184
                 Too many modes input, reduce the number by deleting input
        С
0185
                 eigen list values which have attenuation rates in excess
        С
0186
                 of atnmax and re-count the modes
0187
                 capk=1./(1.-.5*a!pha*h)
0188
                 aconst=-182.0426*freq
0189
                 atnmx=atnmax
0190
        611
                 nm=0
0191
                 do 614 m=1,nmds
0192
                 if(eigen(1,m) .eq. 0.) go to 615
0193
                 theta=cmp|x(eigen(1,m),eigen(2,m))*(.01745329252,0.)
0194
                 if(aconst*aimag(capk*csin(theta)) .le. atnmx) then
0195
                   if (nm .eq. 30) then
0196
                     antmx=atnmx-5.
0197
                     go to 611
0198
                   else
0199
                     nm=nm+1
0200
                     elist(1,nm)=eigen(1,m)
0201
                     elist(2,nm)=eigen(2,m)
0202
                   end if
0203
                 end if
0204
        614
                 continue
0205
        615
                 nmds=nm
0206
                 if(nprint .qt. 1)
0207
                   print 1042, atnmax, (elist(1,k), elist(2,k), k=1, nmds)
              $
0208
               else
0209
                 Keep all input modes.
0210
                 do 616 m=1,nmds
0211
                 elist(1,m)=eigen(1,m)
0212
        616
                 elist(2,m)=eigen(2,m)
0213
               end if
0214
               if (nmds . lt. 30) then
0215
                 elist(1,nmds+1)=0.
0216
                 elist(2,nmds+1)=0.
0217
               end if
0218
        c
0219
               if (rpoly .eq. 1 .and. tlist(1,1) .eq. 0.) then
                 do 619 m=1,nmds
0220
0221
                 tlist(1,m)=elist(1,m)
0222
        619
                 tlist(2,m)=elist(2,m)
0223
               end if
0224
        c
0225
               if (nuflag .eq. 0) then
0226
                 mhtmx=2
0227
                 hclist(1)=200.
0228
                 hclist(2)=0.
```

#### SW\$MAIN

```
0229
                do 641 n=1,nrspec
0230
                en=alog(coefnu(n))
0231
                cflist(1,n)=en+expnu(n)*hclist(1)
        641
0232
                cflist(2,n)=en+expnu(n)+hclist(2)
0233
              end if
0234
        C
0235
              if (nprof .eq. 1) then
0236
                 if (beta*hprime .eq. 0. .and. npath .ne. 2) then
0237
                  This is not a presegmented path, the profile specification
        С
0238
                  must be made in the NAMELIST.
        c
0239
                  print *, 'ABORT MAIN: BETA or HPRIME not input '
0240
                  stop
0241
                end if
0242
                nrspec=1
0243
                 lhtmx=2
0244
                htlist(1)=200.
0245
                htlist(2)=0.
0246
                hprout=hprime
0247
              else
0248
                 if (nprof .eq. 2) then
0249
        С
                  Non-exponential profile, get a value for HPRIME
0250
                  call gethpr(wr0,hprout)
0251
                end if
0252
              end if
0253
        С
0254
        С
              BEGIN:
0255
        С
0256
              call gcpath
0257
              go to 10
0258
        999
0259
              stop
0260
        1000 format(a)
0261
        1001
              format(1x,(a))
0262
        1002
              format(8x, i1)
0263
        1004
              format(8x,a)
0264
        1040 format('Input
                               EIGEN list: D=',f5.2,' H=',f5.2/
0265
                      ' EIGEN =',6(f8.3,' ')/(8x,6(f8.3,' ')))
0266
        1042 format(' Reduced EIGEN list: ATNMAX=',f5.1/
0267
                      ' EIGEN =',6(f8.3,' ')/(8x,6(f8.3,' ')))
0268
              end
```

0001	function cdang(arg)
0002	complex*16 arg
0003	real∗8 cdang,argr,argi
0004	argr=dreal (arg)
0005	argi=dimag(arg)
0006	cdang=datan2(argi,argr)
0007	if(argi .ge. 0.d0) return
8000	cdang=cdang+6.2831853072d0
0009	return
0010	end

```
0001
              subroutine comp f
              implicit real +8 (a-h,o-z)
0002
0003
        С
0004
              include 'common2.for'
               include 'common3.for'
0018
0043
              c=cdcos(theta*zdtr)
0044
0045
              csq=c*c
0046
              s=cdsin(theta*zdtr)
0047
               ssq=s*s
              call rbars
0048
               if(rpoly .eq. 0) then
0049
                 call integ
0050
0051
               else
0052
                 call uspoly
0053
               end if
               if(typitr-1) 5,10,15
0054
        5
               f=(rbar11*r11-zone)*(rbar22*r22-zone)
0055
              $ -rbar11*rbar22*r12*r21
0056
0057
               return
               f=rbar11*r11-zone
0058
        10
0059
               return
               f=rbar22*r22-zone
0060
        15
0061
               return
0062
               end
```

```
0001
               subroutine drvequ
0002
               implicit real *8 (a-h,o-z)
0003
         c
0004
               include 'common1.for'
0020
               include 'common2.for'
               include 'common3.for'
0034
0059
        С
               complex*16 k2i,il,im,in,capd,usqd,yud,ysqd,u,usq,
0060
0061
              $
                           t11, t31, t42, t44, t12vrc, t14vrc, t32vrc, t34vrc, ct41,
              $
0062
                           s11a,d11a,s11b,d11b,c12,c21,
              $
0063
                           s12,d12,s21,d21,s22,d22,b11,b22,b12,b21
0064
               real *8 lsq,msq,nsq,lm,ln,mn
0065
               real +4 ht0
0066
               dimension cx(3), capy(3), ysq(3)
0067
               data dtr/1.745329252d-2/,coeffy/1.758796d11/,coeffx/3.182357d09/
0068
0069
               entry intcmp
0070
               k2i=dcmplx(0.d0,-0.5d0*wn)
0071
               sindip=dsin(codip+dtr)
0072
               drcosl=sindip*dcos(azim*dtr)
0073
               drcosm=sindip*dsin(azim*dtr)
0074
               drcosn=-dcos(codip+dtr)
0075
               il=dcmplx(0.d0,drcosl)
0076
               im=dcmplx(0.d0,drcosm)
0077
               in=dcmplx(0.d0,drcosn)
0078
               lsq=drcosl++2
0079
               msq=drcosm**2
0080
               nsq=drcosn**2
0081
               lm=drcos|*drcosm
0082
               In=drcosl*drcosn
0083
               mn=drcosm*drcosn
0084
               c0=coeffx/omega**2
0085
               cy=coeffy*magfld/omega
0086
               do 1 k=1,nrspec
0087
               cx(k)=c0*charge(k)**2/mratio(k)
0088
               capy(k)=cy*charge(k)/mratio(k)
0089
        1
               ysq(k)=capy(k)**2
0090
               call gethpr(100.*wr0,ht0)
0091
               topht=ht0
0092
               | htmn=| ht
0093
               mhtmn=mht
0094
               if (debug .le. 1) return
0095
               print 110
0096
               I=Ihtmn
0097
               m=mhtmn
0098
               ht=topht
0099
        10
               slopel=(ht-htlist(!+1))/(htlist(!)-htlist(!+1))
0100
               slopem=(ht-hclist(m+1))/(hclist(m)-hclist(m+1))
0101
               ed=dexp(lnlist(l+1,1)+(lnlist(l,1)-lnlist(l+1,1))*slopel)
0102
               en=dexp(cflist(m+1,1)+(cflist(m,1)-cflist(m+1,1))*slopem)
0103
               capx=ed*cx(1)
0104
               capz=en/omega
0105
               wr=omega*capx/capz
0106
               print 111, ht, ed, en, capx, capz, wr
0107
               if (ht .lt. topht) return
0108
               ht=d
0109
               do 11 j=1, |htmx
```

```
DRVEQU
0110
               if (d .ge. htlist(j)) go to 12
               |=j
0111
        11
0112
        12
               do 13 j=m,mhtmx
               if(d .ge. hclist(j)) go to 10
0113
0114
        13
0115
0116
               entry smtrix
0117
               usqd=zero
0118
               yud=zero
0119
               ysqd=zero
0120
               slopel=(ht-htlist(lht+1))/(htlist(lht)-htlist(lht+1))
0121
               slopem=(ht-hclist(mht+1))/(hclist(mht)-hclist(mht+1))
0122
               do 20 k=1,nrspec
0123
               capx=dexp(Inlist(Iht+1,k)
0124
                       +(Inlist(Iht,k)~Inlist(Iht+1,k))*slopel)*cx(k)
0125
               capz=dexp(cflist(mht+1,k)
0126
                       +(cflist(mht,k)-cflist(mht+1,k))*slopem)/omega
0127
               u=dcmp(x(1.d0,-capz))
0128
               usq=u*u
0129
               capd=-capx/(u*(usq-ysq(k)))
0130
               if (cdabs (capd) .gt. 1.d-30) then
0131
                 usqd=usqd+usq*capd
0132
                 yud=yud+capy(k)*u*capd
0133
                 ysqd=ysqd+ysq(k)*capd
0134
               end if
0135
        20
               continue
0136
               crvtrm=alpha*(h-ht)
               m11=usqd-lsq*ysqd-crvtrm
0137
0138
               m22=usqd-msq*ysqd-crvtrm
0139
               m33=usqd-nsq+ysqd-crvtrm
0140
               m12=-in+yud-lm+ysqd
0141
               m21= in+yud-lm+ysqd
0142
               m13= im*yud-In*ysqd
0143
               m31=-im+yud-In+ysqd
0144
               m23=-il+yud-mn+ysqd
0145
               m32= il*yud-mn*ysqd
0146
               capd=zone/(zone+m33)
0147
               t11=-s*m31*capd
0148
               t12vrc=s+m32*capd/c
0149
               t14vrc=(csq+m33)*capd/c
0150
               t31=m23+m31+capd-m21
0151
               t32 vrc = c + (m22 - m23 + m32 + capd)/c
0152
               t34vrc=s+m23+capd/c
               ct41 = (zone+m11-m13+m31+capd) + c
0153
0154
               t42=m32+m13+capd-m12
0155
               t44=-s*m13*capd
0156
               s11a=t11+t44
0157
               dlla=tll-t44
0158
               sl1b=tl4vrc+ct41
0159
               d11b=t14vrc-ct41
0160
               s12=t12vrc+t42
0161
               d12=t12vrc-t42
0162
               s21=t34vrc+t31
0163
               d21=t34vrc-t31
0164
               s22=c+t32vrc
               d22=c-t32vrc
0165
```

0166

C

```
DRVEQU
0167
               if (ht .eq. topht) call intalr
0168
0169
               entry rderiv
0170
               k=0
0171
               do 30 j=1,7,2
0172
               k=k+1
0173
               if(dabs(logr(j)) .gt. 15.d0)
0174
              \frac{1}{2} \log(k) = dcmplx(dsign(15.d0, logr(j)), 0.d0)
0175
        30
               rs(k)=cdexp(logrs(k))
0176
               bl1=r11*(d11a-d11b)
0177
               b22=r22*d22
0178
               b12=r12*d21
0179
               b21=r21*s12
0180
               c12=r12*s21
0181
               c21=r21*d12
0182
               dl11dh=k2i*
0183
                     (b11+b12+b21-s11b-s11b+(r12*r21*d22+c12+c21-d11a-d11b)/r11)
0184
               d122dh=k2i*
0185
                     (b12+b21+b22-s22-s22+(r12*r21*(d11a-d11b)+b12+b21+d22)/r22)
0186
               d112dh=k2i*
0187
                     (b11+b12+b22+s11a-s11b-s22+(r11+s12+d12)+(r22+zone)/r12)
0188
               d121dh=k2i*
0189
                     (b11+b21+b22-s11a-s11b-s22+(r11*d21+s21)*(r22+zone)/r21)
0190
        С
0191
               if (debug .gt. 2) then
0192
                 print 100, ht, delh, logr, dlrdh
0193
               end if
0194
               return
0195
        100
0196
               format(f9.4,1pe12.4,4(1x,2e12.3)/21x,4(1x,2e12.3))
0197
        110
               format(/' Electron density parameters: ht
                                                                          nu',
0198
                       8x, 'x
0199
               format(27x, f7.1, 1p5e10.2)
        111
0200
```

```
0001
              subroutine extrap
0002
        C
0003
              This routine sets up and maintains the data sets for the quadratic
        С
0004
        C
              extrapolation of eigen's down the propagation path.
0005
        c
0006
               include 'common1.for'
0022
               include 'common2.for'
0036
        C
0037
               logical brwstr
0038
              complex*8 t(30),y(30),ys(3,30),s,tb,stb,capk,coeff,ngsq,
0039
                         zero/(0.,0.)/,zone/(1.,0.)/,zmplxi/(0.,1.)/
0040
              dimension xs(3)
0041
              equivalence (elist,y),(tlist,t)
0042
              data dtr/.01745329252/
0043
        С
0044
               if(lx .eq. 0) then
0045
                This is the first point on the propagation path.
        C
0046
                Set up constants and remove input modes with attenuation
        C
                 rates greater than atnmax.
0047
        С
0048
                 capk=cmplx(1.-.5*alpha*h,0.)
0049
                 coeff=cmplx(0.,182.0428*freq)/capk
0050
        C
0051
                Get Brewster mode
        C
0052
                 if (sigma .lt. 1.e-3) then
0053
                   ngsq=cmplx(epsr,-1.7975e7*sigma/freq)
0054
                   stb=csqrt(ngsq/(ngsq+zone))*capk
0055
                   atten=coeff*stb
0056
                   if (atten .le. atnmax) then
0057
                     The Brewster mode is contained within the normal set.
        C
0058
                     tb=(90.,0.)
0059
                     brwstr=.false.
0060
                   else
0061
                    The Brewster mode is outside the normal set.
        С
0062
                     if (atten .le. 2.*atnmax) then
0063
                       The attenuation rate is not excessive.
        С
0064
                       tb=cmp|x(0.,-1./dtr)*clog(csqrt(zone-stb**2)+zmp|xi*stb)
0065
                       brwstr=.true.
0066
                     else
0067
                       The attenuation rate is excessive.
        C
0068
                       tb=(90.,0.)
0069
                       brwstr=.false.
0070
                     end if
0071
                   end if
0072
                 else
0073
                   tb=(90.,0.)
0074
                   brwstr=.false.
0075
                end if
0076
                do 139 k=1,30
0077
                mode(k)=k
0078
        137
                 if (real(y(k)) . gt. 0.) then
0079
                   if (brwstr) then
0080
                    If this mode is near the Brewster, then keep it.
        c
0081
                     if (abs(real(y(k)-tb)) .le. 1. .and.
0082
                        abs(aimag(y(k)-tb)) .le. .5) go to 139
0083
                   end if
0084
                   atten=coeff*csin(y(k)*dtr)
0085
                   if (atten .gt. atnmax) then
```

```
EXTRAP
0086
                     do 138 l=k,30
0087
                     t(l)=t(l+1)
0088
        138
                     y(1)=y(1+1)
0089
                     t(30)=zero
0090
                     y (30) = zero
                     go to 137
0091
0092
                   end if
0093
                 end if
0094
        139
                 continue
0095
                 return
0096
               end if
0097
        c
0098
               x=rho
0099
               if(nprint .gt. 1) print 1000,x
0100
               nmds=1s
0101
               do 143 k=1, nmds
0102
               s=zero
0103
               do 142 | 1=1, | x
0104
               p=1.
0105
               do 141 | 2=1, | x
0106
               if(11 .eq. 12) go to 141
0107
               p=p*(x-xs(12))/(xs(11)-xs(12))
0108
        141
               continue
0109
        142
               s=s+p*ys(11,k)
0110
               if(nprint .gt. 1) print 1001,mode(k),s
0111
               t(k)=s
0112
        143
               y (k) =s
0113
        С
0114
               Scan the extrapolated eigen's for invalid values.
0115
               do 151 k=1,nmds
0116
               if(real(y(k)) .le. 0. .or. real(y(k)) .ge. 90. .or.
0117
              aimag(y(k)) .ge. 0.) then
0118
                 print *, 'ERROR EXTRAP: Extrapolated mode', mode(k)
0119
                 lost=1
0120
                 return
0121
               end if
0122
        151
               continue
0123
               if (nmds .lt. 30) then
0124
                 t(nmds+1)=zero
0125
                 y(nmds+1)=zero
0126
               end if
0127
               return
0128
        c
0129
               entry xsave
0130
        C
0131
        C
               This entry point is called after execution of WVGUID.
0132
        c
               It updates the data sets used to do the quadratic extrapolation.
0133
        С
0134
               x=rho
               if(lx .lt. 3) then
0135
0136
                 |x=|x+1|
```

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0137

0138

0139

0140 0141

0142

21

else

end if

do 21 l=1,2

xs(|)=xs(|+1) do 21 k=1,nmds

ys(i,k)=ys(i+1,k)

```
EXTRAP
0143
0144
```

```
1s=nmds
               xs(|x)=x
               do 25 k=1, nmds
0145
        25
0146
               ys(lx,k)=y(k)
0147
        С
               Keep all eigen's at first input distance.
0148
        C
0149
               if(lx .eq. 1) then
0150
                 modes=nmds
0151
                 return
0152
               end if
0153
               j is counter for modes to be output by SAVEMC
        С
0154
               k is counter for modes to be used by WVGUID
0155
               i=0
0156
               k=1
        251
0157
               if(k .gt. nmds) return
0158
               j=j+1
0159
               if (brwstr) then
0160
                 Check if this mode is near the Brewster; if so, then keep it.
        C
                 if (abs(real(y(k)-tb)) . le. 1. .and.
0161
0162
                    abs(aimag(y(k)-tb)) .le. .5) go to 256
               end if
0163
0164
               atten=coeff*csin(y(k)*dtr)
0165
               if (atten .gt. atnmax) then
0166
                 Delete k-th mode
        C
0167
                 do 253 l=1,4
0168
        253
                 T term(!,j)=zero
0169
                 nmds=nmds-1
0170
                 |s=nmds
0171
                 if (nmds .eq. 0) then
0172
                   print *, 'ERROR EXTRAP: All modes have been deleted'
0173
                   lost=1
0174
                   t(1)=zero
0175
                   y(1)=zero
0176
                   return
0177
                 end if
0178
                 if (k .gt. nmds) then
0179
        257
                   modes=modes-1
0180
                   if(real(T term(1,modes)) .ne. 0.) return
0181
                   go to 257
0182
                 else
0183
                   do 254 l=k,nmds
0184
                   mode(!) = mode(!+1)
0185
                   t(1)=t(1+1)
0186
                   y(1)=y(1+1)
0187
                   do 254 m=1, lx
0188
                   ys(m,l) = ys(m,l+1)
0189
         254
                   continue
0190
                   t(nmds+1)=zero
0191
                   y(nmds+1)=zero
0192
                   go to 251
0193
                 end if
0194
               end if
0195
        256
               k=k+1
0196
               go to 251
0197
0198
        1000
               format(/' Extrapolated EIGEN list for x = ', f8.3)
0199
        1001
               format(i5,5x,2f8.3,f12.3)
0200
               end
```

```
0001
                 subroutine gcdbr(d1,clt1,clt2,rho,br,inb)
0002
        c
0003
        С
                 Returns great circle distance and geographic bearing angle
0004
        C
0005
        C
                         DL is longitude of point 2 minus longitude of point 1
0006
                         CLT1 is co-latitude of point 1
        C
0007
                         CLT2 is co-latitude of point 2
        C
8000
                         INB=0: RHO is computed and
        C
0009
                                  BR from point 1 thru point 2 is computed at 1
        C
0010
        c
                         INB=1:
                                 RHO is input
                                                  and
0011
                                 BR from point 1 thru point 2 is computed at 2
        ¢
0012
        C
0013
                          RHO is great circle distance between the input points
        C
                 Output:
0014
                          BR is geographic bearing angle measured clockwise from
        C
0015
                                  due North
        C
0016
        C
0017
                 All coordinates, RHO and BR are in radians
        C
0018
                 Sign convention is + for West and North
        c
0019
0020
                 data pi/3.14159265e0/,twopi/6.28318531e0/
0021
        C
0022
                 reduce(arg)=sign(amin1(abs(arg),1.),arg)
0023
        c
0024
                 cc|t1=cos(c|t1)
0025
                 sclt1=sin(clt1)
0026
                 cclt2=cos(clt2)
0027
                 sclt2=sin(clt2)
0028
        C
0029
                 adl=abs(dl)
0030
                 if (adl.ge.pi) then
                   dl=amod(dl,twopi)
0031
0032
                 else
0033
                   adl=abs(dl)
0034
                 end if
0035
                 if (inb .eq. 1) then
0036
                   if(rho .gt. pi) then
0037
                     gcd=twopi-rho
0038
                   else
0039
                     gcd=rho
0040
                   end if
0041
                 end if
0042
                 if (abs(clt1) .le. 1.e-6 .or. abs(clt1-pi) .le. 1.e-6) go to 10
0043
                 if (adl .le. 1.e-6) go to 20
0044
                 if (abs(adl-pi) .le. 1.e-6) go to 30
0045
                 if (adl.ge.pi) then
0046
                   if(dl .ge. 0.) then
0047
                     dl=dl-twopi
0048
                   else
0049
                     dl=dl+twopi
0050
                   end if
0051
                 end if
0052
                 if (inb .eq. 0) then
0053
                   cgcd=cclt1*cclt2+sclt1*sclt2*cos(dl)
0054
                   gcd=acos(reduce(cgcd))
0055
                   if (abs(cgcd-1.) .le. 1.e-6) then
0056
                     br=0.
0057
                   else
```

```
GCDBR
0058
                     br=acos(reduce((cclt2-cclt1*cgcd)/(sclt1*sin(gcd))))
0059
                   end if
0060
                else
0061
                   if (abs(gcd) .le. 1.e-6) then
0062
                     br=0.
0063
                   else
0064
                     br=pi-acos(reduce((cclt1-cclt2*cos(gcd))/(sclt2*sin(gcd))))
0065
                   end if
0066
                 end if
0067
                 if(dl .lt. O.) br=twopi-br
0068
                 go to 40
0069
        C
0070
                 point 1 is at one of the poles
        C
        10
0071
                 if (inb .eq. 0) gcd=abs(clt1-clt2)
0072
                 if (abs(clt1) .le. 1.e-6) then
0073
                   br=pi-dl
0074
                 else
                   br=d1
0075
                 end if
0076
0077
                 go to 40
0078
        С
0079
                 coordinates are on same longitude
0080
        20
                 dc=c|t1-c|t2
0081
                 if (dc .ge. 0.) then
0082
                   br=0.
0083
                 else
0084
                   dc=-dc
0085
                   br=pi
0086
                 end if
0087
                 if (inb .eq. 0) gcd=dc
0088
                 go to 40
0089
        С
0090
                 coordinates are on opposite longitudes
        С
0091
        30
                 dc=c|t1+c|t2
0092
                 if (dc .le. pi) then
0093
                   if(inb .eq. 0) then
0094
                     br=0.
0095
                   else
0096
                     br=pi
0097
                   end if
0098
                 else
0099
                   dc=twopi-dc
0100
                   if (inb leq. 0) then
0101
                     br=pi
0102
                   else
0103
                     br=0.
0104
                   end if
0105
                 end if
0106
                 if (inb .eq. 0) gcd=dc
0107
        С
0108
                 long path calculations
0109
        40
                 if (inb .eq. 1) then
0110
                   if (rho .gt. pi) then
0111
                      if(br .lt. pi) then
0112
                       br=br+pi
0113
                     else
0114
                       br=br-pi
```

```
0001
              subroutine gcpath
0002
        С
0003
              sign convention: + for west and north, - for east and south
        c
0004
0005
               include 'common1.for'
              include 'common2.for'
0021
0035
        С
0036
              dimension prof1(50,3),prof2(50,3)
0037
              real ing, long, lat, m1, m2, mgf
0038
              character * 72 bcd, preseg
0039
              logical first
0040
              data dtr/1.745329e-2/,re/6.366/,alt/80./
0041
        C
0042
              min=0 --- normal
        C
0043
                 =1 --- interpolating between preseg values
0044
                 =2 --- last interpolation interval
0045
        c
0046
               lost=0 -- no trouble with modes
        С
                   =1 -- dropped a mode in WVGUID or EXTRAP
0047
        c
0048
                   =2 -- all modes found but one or more changed significantly
0049
        С
                         from the extrapolated values
0050
        C
0051
              nprof=0 - use profile from MAIN
        С
0052
                     1 - use exponential profile
        С
0053
        С
                     2 - read non-exponential profiles along path
0054
                         WARNING: the heights must match in each profile
        С
0055
        С
0056
              first=.true.
               write(90,*) 'Failure at RHO 1'
0057
0058
        C
0059
               1x=C
0060
              min=0
0061
              bta=0.
0062
               sig=0.
0063
               mgf=0.
0064
               sigma1=0.
0065
               tlng=tlong*dtr
0066
               tclt=(90.-tlat)*dtr
0067
               rho0=rho
0068
               rhop=rho
0069
               drho=drmin
0070
               if (rbear .eq. 720.) then
0071
                 call gcdbr((tlong-rlong)*dtr,tclt,(90.-rlat)*dtr,gcd,xtr,0)
0072
                 brng=xtr/dtr
0073
                 if (igcd .eq. 1) then
0074
                   rhomax=gcd*re
0075
                 else
0076
                   rhomax=dmax
0077
                 end if
0078
               else
0079
                 xtr=rbear*dtr
0080
                 brng=rbear
0081
                 rhomax=dmax
0082
               end if
0083
        c
0084
        20
               if (npath .eq. 2) then
0085
                 Presegmented path
```

```
0086
                 read(5,2000,end=900) preseg
0087
                 read(preseg,*) rho,azm,cdp,mgf,sig,eps,bta,hprm
                 if(rho .eq. 40.) then
0088
                   print *, 'End of preseg data'
0089
                   rewind 90
0090
0091
                   write(90,2003)
0092
                   go to 999
0093
                 else if (rho .gt. rhomax) then
0094
                   print *, 'DMAX reached before end of preseg data '
0095
                   rewind 90
0096
                   write(90,2003)
0097
                   go to 900
0098
                 end if
0099
                 if(first) then
0100
                   rho0=rho
0101
                   rhop=rho
0102
                 end if
0103
                 drho=rho-rhop
0104
                 if (drho .lt. O.) then
0105
                   print *, 'ABORT GCPATH: Preseg rhos out of order'
0106
                   go to 900
0107
                 end if
0108
                 if (nprof .eq. 2) then
0109
                   read(3,2000) bcd
0110
                   if (bcd(1:8) .ne. 'profile' .and.
              $
                      bcd(1:8) .ne. 'PROFILE') then
0111
                     print *,'ABORT GCPATH: PROFILE control string missing'
0112
                     go to 900
0113
0114
                   end if
0115
                   read(bcd, 2001) nn
                   if (nrspec .ne. maxO(1,nn)) then
0116
                     print *,'ABORT GCPATH: Number of species is incorrect'
0117
                     go to 900
0118
0119
                   end if
0120
                   call profin(3,1,50,nprint,nrspec,lhtmx,htlist,lnlist)
0121
                   if(lhtmx .lt. 0) then
                     print *, 'ABORT GCPATH: Profile missing'
0122
0123
                     go to 900
0124
                   end if
0125
                   if(|htmx .gt. 0) then
0126
                     if (lhtmx .ne. lhtmx1) then
0127
                       print *,'ABORT GCPATH: Number of heights is incorrect'
0128
                       go to 900
0129
                     end if
0130
                     call gethpr(wr0,hprout)
0131
                   end if
                 else
0132
0133
                   if(nprof .eq. 1) then
0134
                     if (bta .gt. 0.) then
0135
                       beta=bta
0136
                       hprime=hprm
0137
0138
                     if (beta*hprime .eq. 0.) then
0139
                       print *, 'ABORT GCPATH: BETA or HPRIME not input'
0140
                       go to 900
0141
                     end if
0142
                   end if
```

```
GCPATH
0143
                   Calculate exponential profile:
        c
0144
                   Inlist(1,1)=cflist(1,1)+beta*(htlist(1)-hprime)-9.4517306
0145
                   lnlist(2,1)=cflist(2,1)+beta*(htlist(2)-hprime)-9.4517306
0146
                   hprout=hprime
0147
                 end if
0148
              end if
0149
        C
0150
               if (npath .eq. 1) then
0151
                 Calculate midpoint distance:
        С
0152
                 rho=.5*rhomax
              else
0153
0154
                 if (rho .eq. 0.) then
0155
                   Begin at xmtr
        С
0156
                   Ing=ting
0157
                   clt=tclt
0158
                   br=xtr
0159
                 end if
0160
               end if
0161
0162
        30
               if (rho .gt. 0.) then
                 gcd=rho/re
0163
0164
                 call recvr(tlng,tclt,xtr,gcd,lng,clt)
0165
                 if (rho .eq. 20.) then
0166
                   At the antipode of the transmitter.
        C
0167
                   br=9.4247779608-xtr
0168
                   if (br .gt. 6.2831853072) br=br-6.2831853072
0169
0170
                   call gcdbr(tlng-lng,tclt,clt,gcd,br,1)
0171
                 end if
0172
               end if
0173
               bpath=br/dtr
0174
               long=Ing/dtr
0175
               colat=clt/dtr
0176
               lat=90.-colat
0177
        c
               if(sig .gt. 0.) then
0178
0179
                 sigma=sig
0180
                 epsr=eps
0181
               else
0182
                 if(ignd .eq. 1) call ground(long, lat, ncode, sigma, epsr)
0183
0184
               If conductivity has changed, then restart extrapolation
        C
0185
               if (sigmal .ne. sigma .and. sigmal .ne. 0.) then
                 min=0
0186
0187
                 1x=0
0188
                 call xsave
0189
                 1x=0
0190
               end if
0191
        c
0192
               if (mgf .gt. 0.) then
0193
                 azim=azm
0194
                 codip=cdp
0195
                 magf|d=mgf
0196
                 if(magfld .gt. 1.e-02) magfld=magfld+1.e-04
0197
               else
0198
                 call newmag(0,alt,lng,clt,bmf,dip,b,br,bp,bt)
```

azim=bpath-bmf/dtr

```
0200
                 if (azim .lt. O.) then
0201
                   azim=azim+360.
0202
                 else if (azim .gt. 360.) then
                   azim=azim-360.
0203
0204
                 end if
                 codip=90.-dip/dtr
0205
0206
                 magf | d=b+1.0e-04
0207
0208
                 if (mdir .eq. 1) then
0209
                   Reverse azim if contours for xmtr deployment
        C
0210
                   azim=azim-180.
                   if (azim . It. O.) then
0211
0212
                     azim=azim+360.
                   else if (azim .gt. 360.) then
0213
0214
                     azim=azim-360.
0215
                   end if
0216
                 end if
0217
        c
0218
               end if
               print 1000, rho, long, lat, bpath, azim, codip, magfld, sigma, epsr
0219
0220
        40
0221
               lost=0
0222
               x=rho
0223
               call extrap
0224
               if(lost .eq. 1) go to 100
0225
               call wvguid
0226
               if (nmds .eq. 0 .and. (rho .eq. 0. .or. npath .eq. 1 )) then
0227
                 print *, 'ABORT GCPATH: Failure at starting rho'
0228
                 go to 900
0229
               end if
0230
               if(lost .eq. 1) go to 100
0231
               call xsave
0232
               if(lost .eq. 1) go to 100
0233
               rhop=rho
0234
               if(min .eq. 1) go to 50
0235
               if(first) then
0236
                 Primary output file:
        C
0237
                 open(unit=lunit7,status='new')
0238
                 if (year .eq. 0 .and. month .eq. 0 .and. day .eq. 0) then
                   write(lunit7,1030) tlong, tlat, brng, beta, hprime, pathid
0239
0240
0241
                   write(lunit7,1031) tlong, tlat, brng, beta, hprime,
0242
                                       mod (year, 100), month, day, gmt, pathid
0243
                 end if
0244
                 first=.false.
0245
               end if
0246
               call savemo
0247
               if (npath .eq. 1) then
0248
                 rewind 90
0249
                 write(90,2003)
0250
                 go to 999
0251
               else
0252
                 prowind 90
0253
                 wr.ce(90,2002) rho
0254
0255
               if(rho+.002 .ge. rhomax) go to 900
0256
```

**GCPATH** 

```
GCPATH
0257
               rho1=rho
0258
               a1=azim
0259
               c1=codip
0260
               m1=magfld
0261
               e1=epsr
0262
               s1=alog(sigma)
0263
               sigmal=sigma
               if(nprof .gt. 0) then
0264
0265
                 lhtmx1=lhtmx
0266
                 do 48 l=1, lhtmx
                 do 48 m=1,nrspec
0267
        48
0268
                 prof1(l,m)=Inlist(l,m)
0269
               end if
0270
               if (min .eq. 2) then
0271
                 min=0
                 go to 70
0272
               end if
0273
0274
0275
        50
               if(lost .eq. 2) then
0276
                 if (min .eq. 0) then
0277
                   drho=amax1(drho-drmin,drmin)
0278
0279
                   drho=.5*(rho2-rho)
0280
                 end if
0281
               else
0282
                 if (min .eq. 0) then
0283
                   drho=amin1 (drho+drmin, drmax)
0284
                 else
0285
                   drho=rho2-rho
0286
                 end if
0287
               end if
0288
0289
         70
               if (min .eq. 0 .and. npath .eq. 2) go to 20
0290
               rho=rho+drho
0291
               if(rho+.002 .gt. rhomax) then
0292
                 drho=drho-rho+rhomax
0293
                 rho=rhomax
0294
               end if
0295
               if (min .eq. 1) go to 120
0296
               go to 30
0297
0298
               Back up on propagation path
         С
0299
         100
               if(rho .eq. rho0) then
print *,'ABORT GCPATH: Failure at starting rho'
0300
0301
                 go to 900
0302
               end if
0303
               if (min-1) 101,102,103
0304
         101
               if (npath .eq. 2) go to 105
0305
               if (drho .le. drmin) go to 110
0306
               nrd=.5*drho/drmin
               if(nrd .eq. 0) go to 110
0307
0308
               drho=nrd+drmin
0309
               rho=rho1+drho
```

0311

0312

0313

103

102

go to 30

drho=drhop

drho=.5\*drho

min=1

```
GCPATH
0314
               if (drho .lt. .015125) then
0315
                 print *, 'ABORT GCPATH: Backup interval is less than 0.015125'
0316
                 go to 900
0317
               end if
        104
0318
               rho=rhop+drho
0319
               go to 120
0320
        105
0321
               if((rho-rho1)/drmin .gt. 10.) then
0322
                 print *, 'ABORT GCPATH: Preseg interval too large for efficient
0323
              $processing'
0324
                 go to 900
0325
               end if
0326
        C
0327
               Begin interpolation
        C
0328
        110
               min=1
0329
               drho=.5*(rho-rho1)
0330
               if (drho .lt. .015125) then
0331
                 print *, 'ABORT GCPATH: Backup interval is less than 0.015125'
0332
                 go to 900
0333
               end if
0334
               rho2=rho
0335
               a2=azim
0336
               if (a2-a1 .gt. 180.) then
0337
                 a2=a2-360.
0338
               else if (a2-a1 .lt. -180.) then
0339
                 a2=a2+360.
0340
               end if
0341
               c2=codip
0342
               m2=magfld
0343
               e2=epsr
0344
               s2=alog(sigma)
0345
               sigma2=sigma
0346
               if(nprof .gt. 0) then
0347
                 lhtmx2=lhtmx
0348
                 do 111 l=1, | htmx
0349
                 do 111 m=1,nrspec
0350
        111
                 prof2(l,m)=Inlist(l,m)
               end if
0351
0352
               rho=rho1+drho
0353
        C
0354
        120
               if (rho+.002 .ge. rho2) then
0355
                 End of interpolation
0356
                 min=2
0357
                 drhop=drho
0358
                 drho=drmin
0359
                 rho=rho2
0360
                 azim=a2
0361
                 if (azim .lt. 0.) then
0362
                   azim=azim+360.
0363
                 else if (azim .gt. 360.) then
0364
                   azim=azim-360.
0365
                 end if
                 codip=c2
0366
0367
                 magfld=m2
0368
                 epsr=e2
0369
                 sigma=sigma2
```

if (nprof .gt. 0) then

```
GCPATH
                   do 121 |=1,|htmx
0371
0372
                    do 121 m=1,nrspec
                    Inlist(I,m)=prof2(I,m)
0373
        121
0374
                 end if
0375
               else
0376
                 Interpolate
        c
0377
                 slope=(rho-rho1)/(rho2-rho1)
0378
                 azim=a1+slope*(a2-a1)
0379
                 if (azim . lt. 0.) then
0380
                    azim=azim+360.
0381
                 else if (azim .gt. 360.) then
                    azim=azim-360.
0382
                 end if
0383
                 codip=c1+slope*(c2-c1)
0384
0385
                 magfld=m1+slope*(m2-m1)
0386
                 epsr=e1+slope*(e2-e1)
                 sigma=exp(s1+slope*(s2-s1))
0387
0388
                 if (nprof .gt. 0) then
0389
                    do 122 l=1, lhtmx
0390
                    do 122 m=1,nrspec
         122
0391
                    lnlist(l,m)=prof1(l,m)+slope*(prof2(l,m)-prof1(l,m))
0392
                 end if
0393
               end if
0394
               print 1002,
                              rho, azim, codip, magfld, sigma, epsr
0395
               go to 40
0396
         900
0397
               if (npath .eq. 2) then
                 read(5,2000,end=999) bcd
0398
         903
0399
                 if (bcd(1:5) eq. '40,0,') go to 999
0400
                 go to 903
               end if
0401
0402
         999
               write(lunit7,1032)
0403
               close(unit=lunit7)
               print *, 'Execution terminating for this path'
0404
0405
0406
04(-7
         1000 format(/' Propagation path parameters:
                                                                                 lat'
                                                            rho
                                                                      long
                                                                                epsr'/
0408
                       4x,'bear
                                                        magfld
                                     azim
                                               codip
                                                                     sigma
                       26x,f10.3,f10.2,4f9.2,e11.2,1pe11.2,0pf8.2)
0409
0410
         1002 format(/11x,' Interpolated path parameters:
                                                                 rho
                                                                           azim',
0411
                       5x,'codip
                                     magfld
                                                 sigma
0412
                       38x,f10.3,f10.2,f9.2,e11.2,1pe11.2,0pf8.2)
                             xmtr',f7.1,2f6.1,' prof',f5.2,f5.1/a80)
xmtr',f7.1,2f6.1,' prof',f5.2,f5.1,
0413
         1030
               format('sw
         1031
              format('sw
0414
                          (',3(i2.2,'/'),f4.1,')'/a80)
0415
               format('r 40.')
0416
         1032
               format(a72)
0417
         2000
               format(8x, i1)
0418
         2001
0419
               format(f6.3)
         2002
               format('40')
0420
         2003
0421
                end
```

```
0001
              subroutine gethpr(wr,hpr)
0002
        C
0003
        С
              Routine to determine the height where omega sub r is a
0004
        С
              specific value. The value returned is to nearest km.
0005
        С
0006
              include 'common1.for'
0022
        С
              data coeffx/3.182357e9/
0023
0024
        c
0025
              Start at the bottom of the profile and work up.
        С
0026
        С
0027
              lht=|htmx-1
0028
              mht=mhtmx-1
0029
              ht=amin1(htlist(lhtmx),hclist(mhtmx))
0030
        10
              if(lht .gt. 1 .and. ht .ge. htlist(lht-1)) then
0031
                 lht=lht-1
                go to 10
0032
              end if
0033
0034
        12
               if (mht .gt. 1 .and. ht .ge. hclist(mht-1)) then
0035
                mht=mht-1
                go to 12
0036
0037
              end if
0038
              slope !=(ht-htlist(!ht+1))/(htlist(!ht)-htlist(!ht+1))
0039
              slope m=(ht-hclist(mht+1))/(hclist(mht)-hclist(mht+1))
0040
              sum=0.
0041
              do 14 n=1,nrspec
0042
              dn=exp(Inlist(Iht+1,n)+(Inlist(Iht,n)-Inlist(Iht+1,n))*slope | )
0043
              cf=exp(cflist(mht+1,n)+(cflist(mht,n)-cflist(mht+1,n))*slope m)
0044
        14
              sum=sum+coeffx*dn/(mratio(n)*cf)
0045
              if(sum .gt. wr) then
0046
                hpr=ht
0047
                 if (nprint .gt. 1) then
0048
                   print *
0049
                   print *,'GETHPR: wr, hpr=',wr,hpr
0050
                end if
0051
                return
0052
              end if
0053
              ht=ht+1.
0054
              go to 10
0055
              end
```

```
0001
                subroutine ground(xlong,xlat,ncode,sigma,epsr)
0002
        c
0003
                Returns conductivity code, conductivity, dielectric constant
        c
0004
        С
0005
                Input: XLONG is West longitude in degrees
        С
                         (i.e., -117.3 for 117 degrees, 18 minutes East)
0006
        С
0007
                         XLAT is North latitude in degrees
        C
8000
                        (i.e., 32.8 for 32 degrees, 48 minutes North)
        C
0009
        С
0010
                          NCODE is conductivity code from GRNDMAP.DAT
        c
0011
                          (ncode=0 is sea water, =1 is ice; see DATA below)
        C
0012
                          SIGMA is mho/m
        С
0013
                          EPSR is the dielectric constant
        C
                          A list of sigma and epsr is also placed into a common.
0014
        С
0015
        C
0016
                Requires: GRNDMAP.DAT
        С
0017
0018
                 include '[305021.jaflib]data files.for/list'
0019
                character *40 grnd$d/'user$disk$3:[305021.jaflib]grndmap.dat'/
     1
                character *40 itsn$d/'user$disk$3:[305021.jaflib]itsnoise.dat'/
0020 1
                character *40 wrld$d/'user$disk$3:[305021.jaflib]world.dat'/
0021
      1
0022
        c
0023
                common/grnd$/sss(10),rrr(10)
0024
                 logical first/.true./
0025
                dimension !code(361),map(4530),ss(10),rr(10)
0026
                data ss/1.e-5,3.e-5,1.e-4,3.e-4,1.e-3,3.e-3,1.e-2,3.e-2,.1,4./
0027
                data rr/5.,5.,10.,10.,15.,15.,15.,15.,80.,81./
0028
                 if(first) then
0029
                   open(unit=8, file=grnd$d, status='old', readonly)
0030
                   read(8,1) | code, map
                  format(9i8)
0031
0032
                  close(unit=8)
0033
                   do 2 = 1,10
0034
                   sss(|)=ss(|)
0035
                   rrr(1)=rr(1)
0036
                   first=.false.
0037
                end if
0038
                phi=xlong
                 if (phi .gt. 180.) then
0039
0040
                   phi≔phi-360.
0041
                 else
0042
                   if (phi .lt. -180.) phi=phi+360.
0043
0044
                 if (abs(phi) .gt. 180. .or. abs(xlat) .gt. 90.01) then
0045
                   print 11, xlong, xlat
0046
        11
                   format(/' ******* Error in GROUND: Xlong
                                                                      Xlat'
0047
                          /26x,2f9.2)
0048
                   stop
0049
                end if
0050
                 |at=181.-2.*x|at
0051
                 if (lat .gt. 360) lat=360
0052
                 long=361.-2.*phi
0053
                 if (long .gt. 720) long=1
                 11=|code(lat)
0054
0055
                 |2=|code(|at+1)-1|
                do 21 l=11,12
0056
0057
                maplm1=map(1)/10000
```

```
GROUND
0058
                mapl=map(l)-10000*map!m1
0059
                mlong=mapl/10
0060
                if (mlong .ge. long) go to 31
0061
        21
                continue
0062
        31
                ncd=mapl-mlong+10
0063
                mlong=maplm1/10
0064
                if (mlong .lt. long) go to 41
0065
                ncd=maplm1-mlong*10
0066
        41
                if (ncd .lt. 0 .or. ncd .gt. 9) then
0067
                  print 51,xlong,xlat,long,lat,l1,l2,mlong,ncode
                  format(/, ****** Error in GROUND: Xlong
0068
        51
                                                                    Xlat',
                            long lat
0069
                                         11
                                                 12
                                                     mlong
                                                              ncode'
0070
             5
                         /26x,2f9.2,4i6,2i8)
0071
                  stop
                end if
0072
                ncode=ncd
0073
                if (ncode .eq. 0) ncode=10
0074
0075
                sigma=ss(ncode)
                epsr= rr(ncode)
0076
0077
                return
0078
                end
```

```
0001
               subroutine intalr
0002
               implicit real +8 (a-h,o-z)
0003
        C
0004
               include 'common2.for'
               include 'common3.for'
0018
0043
        C
0044
               complex+16 q,p,t,d11,d13,d31,d33,delta,fnsq,froot,
0045
                          com1,com3,csqm22,csqm33,b3,b2,b1,b0
0046
               dimension phase 1(8), phase 2(8), p(2), t(2), q(4)
0047
               equivalence (logr11,phase1(1))
0048
               data pi/3.141592653d0/, twopi/6.283185307d0/
0049
0050
               if(isotrp-1) 10,100,102
        10
0051
               com1=zone+m11
0052
               com3=zorie+m33
0053
               csqm22=csq+m22
0054
               csqm33=csq+m33
0055
               b3=0.25d0*s*(m13+m31)/com3
0056
               b2=(-csqm33*com1+m13*m31-com3*csqm22+m23*m32)/(6.d0*com3)
               b1=s*(m12*m23+m32*m21-csqm22*(m13+m31))/(4.d0*com3)
0057
0058
               b0=(com1*csqm22*csqm33+m12*m23*m31+m32*m21*m13-m13*m31*csqm22
0059
                        -com1*m23*m32-m12*m21*csqm33)/com3
0060
               call gartic(q,b3,b2,b1,b0,debug,newg)
0061
        c
0062
               do 30 n=1.2
0063
               d11=zone+m11-q(n)**2
0064
               d13=m13+s*q(n)
0065
               d31=m31+s*q(n)
0066
               d33=zone+m33-s**2
0067
               de | ta=d11*d33-d13*d31
0068
               p(n) = (-m12*d33+d13*m32)/delta
0069
               t(n)=q(n)*p(n)-s*(-d11*m32+m12*d31)/delta
0070
               pyntng=t(n)*dconjg(p(n))*q(n)
0071
               if(pyntng .lt. 0.) print 201,theta,q(n),pyntng
        30
0072
               continue
               de|ta=(t(1)*c+p(1))*(c+q(2))-(t(2)*c+p(2))*(c+q(1))
0073
0074
               r11 = ((t(1)*c-p(1))*(c+q(2))-(t(2)*c-p(2))*(c+q(1)))/delta
0075
               r22 = ((t(1)*c+p(1))*(c-q(2))-(t(2)*c+p(2))*(c-q(1)))/delta
0076
               r12 = -2.d0*c*(t(1)*p(2)-t(2)*p(1))/delta
0077
               r21 = -2.d0*c*(q(1)-q(2))/delta
0078
        40
               logr11=cdlog(r11)
0079
               logr12=cdlog(r12)
0080
               logr21=cdlog(r21)
               logr22=cdlog(r22)
0081
0082
               if (adjflg .eq. 1) then
0083
                 do 70 n=2,8,2
0084
        50
                 if(phase1(n)-phase2(n) .le. pi) go to 60
0085
                 phasel(n)=phasel(n)-twopi
0086
                 go to 50
0087
        60
                 if (phase2(n)-phase1(n) .le. pi) go to 70
0088
                 phase1(n)=phase1(n)+twopi
0089
                 go to 60
        70
0090
                 continue
0091
               end if
0092
               do 90 n=2,8,2
0093
        90
               phase2(n)=phase1(n)
0094
               if (debug .gt. 2) print 202
```

## INTALR

```
0095
              return
0096
        100
0097
              ir=1
              fnsq=zone+m11
0098
              froot=cdsqrt(csq+m11)
0099
0100
              go to 106
        101
              r11=(fnsq*c-froot)/(fnsq*c+froot)
0101
              r22=(c-froot)/(c+froot)
0102
              go to 105
0103
0104
        102
              ir=2
0105
0106
              fnsq=zone+m11
              froot=cdsqrt(csq+m11+m13**2/fnsq)
0107
0108
              go to 106
        103
              com1=(s*froot+m13)/(s*fnsq+m13)
0109
0110
              r11=(c-com1)/(c+com1)
              ir=3
0111
              froot=cdsqrt(csq+m22)
0112
0113
              go to 106
0114
        104
              r22=(c-froot)/(c+froot)
        105
              r12=(1.d-20,0.d0)
0115
              r21=(1.d-20,0.d0)
0116
0117
              go to 40
0118
        C
        106
0119
              if (dimag(froot) .gt. 0.d0) froot=-froot
0120
               if(ir-2) 101,103,104
0121
              format(' for theta=',f7.4,f9.4,' q=',1p2e11.3,
        201
0122
                        poynting(z)=',e11.3)
0123
0124
        202
              format(/4x,'ht',7x,'delh')
0125
              end
```

```
0001
               subroutine integ
0002
               implicit real +8 (a-h,o-z)
0003
        C
0004
               include 'common1.for'
               include 'common2.for'
0020
0034
               include 'common3.for'
0059
        C
0060
               real *8 logr0
0061
               integer sflag
0062
               dimension logr0(8), dlrdh0(8), dlogr0(8), dlogr1(8), dlogr2(8)
0063
               data dlhmin/1.953125d-3/,dlgrmx/1.d20/
0064
        C
               factor=10.d0**(-prec)
0065
0066
               emax=factor *3.d0
0067
               emin=factor*.3d0
0068
               ht=topht
0069
               iht≈ihtmn
0070
               mht=mhtmn
0071
               delh=3.125d-2
0072
               svdelh=delh
               if (debug .gt. 2) print 200, theta
0073
0074
               call smtrix
0075
         C
0076
               runge kutta
0077
         10
               sflag=0
               if (debug .gt. 2) print 201
0078
0079
         11
               if(lht .lt. lthmx .and. ht .le. htlist(lht+1)) then
0080
                 lht=lht+1
                 go to 11
0081
0082
               end if
0083
         13
               if (mht .lt. mthmx .and. ht .le. hclist(mht+1)) then
0084
                 mht=mht+1
0085
                 go to 13
0086
               end if
0087
               if (ht-delh .lt. htlist(lht+1)) then
0088
                 sf lag=1
0089
                 saveht=htlist(|ht+1)
0090
                 delh=ht-saveht
0091
               end if
0092
               if (ht-delh .lt. d) then
0093
                 sflag=1
0094
                 saveht=d
                 delh=ht-saveht
0095
0096
               end if
0097
               do 30 i=1.8
0098
               logr0(i)=logr(i)
0099
         30
               dlrdhO(i)=dlrdh(i)
0100
         C
               Try again
0101
         С
0102
         40
               do 50 i=1,8
0103
               dlogr0(i)=-dlrdh0(i)*delh
0104
         50
               logr(i) = logr0(i) + 0.5d0 + dlogr0(i)
               ht=ht-0.5d0+delh
0105
0106
               call smtrix
0107
               do 60 i=1.8
0108
               dlrdh(i)=dsign(dmin1(dlgrmx,dabs(dlrdh(i))),dlrdh(i))
0109
               dlogr1(i)=-dlrdh(i)*delh
```

```
INTEG
0110
        60
               logr(i) = logr0(i) + 0.5d0 * dlogr1(i)
0111
               call rderiv
0112
               do 70 i=1.8
0113
               dIrdh(i)=dsign(dmin1(dlgrmx,dabs(dIrdh(i))),dIrdh(i))
0114
               dlogr2(i)=-dlrdh(i)*delh
        70
0115
               logr(i)=logr0(i)+dlogr2(i)
0116
               ht=ht-0.5d0+delh
0117
               call smtrix
0118
               error=0.d0
               do 80 i=1.8
0119
0120
               dlrdh(i)=dsign(dmin1(dlgrmx,dabs(dlrdh(i))),dlrdh(i))
0121
               d\log 4 = ((-dlrdh(i) + delh + dlogr0(i))/2.d0 + dlogr1(i) + dlogr2(i))/3.d0
0122
               logr(i)=logr0(i)+dlogr4
        80
0123
               error=error+(dlogr2(i)-dlogr4)**2
0124
               error=dsqrt(error/8.d0)
0125
               if (error .lt. emax .or. delh .le. dlhmin) go to 100
0126
               sflag=0
0127
               ht=ht+delh
0128
               delh=0.5d0+delh
0129
               if (delh . lt. dlhmin) delh=dlhmin
0130
               go to 40
        100
0131
               call rderiv
0132
               if (error .1t. emin) delh=2.*delh
0133
               if (sflag .eq. 1) then
0134
                 delh=svdelh
0135
                 ht=saveht
               end if
0136
0137
               svdelh=delh
0138
               if(ht .gt. d) go to 10
0139
               return
0140
        200
               format(/' DEBUG: theta =',2f9.4)
0141
               format(''')
        201
0142
0143
               end
```

```
0001
               subroutine iterat
0002
               implicit real *8 (a-h,o-z)
0003
        c
0004
               This routine drives the iteration to obtain solutions to the
        С
0005
               modal equation.
        С
0006
        C
0007
               include 'common2.for'
0021
               include 'common3.for'
0046
        С
0047
               complex*16 theta0,f0,dlthta
0048
               real *4 absr.absi
0049
        c
0050
               nriter=0
0051
               if (debug .gt. 1) then
0052
                 if(rpoly .eq. 0) then
0053
                   print 300
0054
                 else
0055
                   print 301
0056
                 end if
0057
                 print 302
0058
               end if
0059
        C
               Store the starting angle
0060
               theta0=theta
0061
        10
               theta=theta-dthta
0062
               call comp f
0063
               f0=f
0064
               theta=theta+dthta
0065
               call comp f
0066
               Store the magnitude of the f-function for the starting angle
0067
               if(nriter .eq. 0) fmag0=cdabs(f)
0068
               nriter=nriter+1
0069
               dfdtht=(f-f0)/dthta
0070
               d!thta=-f/dfdtht
0071
               if (debug .gt. 1) then
0072
                 fmag=cdabs(f)
0073
                 print 303, theta, fmag, dlthta, dfdtht
0074
               end if
0075
0076
               absr=dabs(dreal(dithta))
0077
               absi=dabs(dimag(dlthta))
0078
               if(absr .gt. thtinc) dlthta=dlthta*(thtinc/absr)
0079
               if(absi .gt. thtinc) dlthta=dlthta*(thtinc/absi)
0080
               theta=theta+dlthta
0081
               if (nriter . It. maxitr .and.
0082
              $ (absr .gt. lub(1) .or. absi .gt. lub(2))) go to 10
0083
        C
0084
               nriter=nriter+1
0085
               f0=f
0086
               call comp f
0087
               dfdtht=(f-f0)/dlthta
8800
               if (debug .gt. 1) then
0089
                 fmag=cdabs(f)
0090
                 d|thta=zero
0091
                 print 303, theta, fmag, dlthta, dfdtht
0092
               end if
0093
               if (rpoly .eq. 1) then
0094
                 Test the magnitude of the f-function of the final angle
```

```
ITERAT
0095
                  fmag=cdabs(f)
                  if (\bar{f}mag .g\dot{t}. fmag0) then
0096
                    print 304, fmag0, fmag
0097
8000
                    theta=theta0
0099
                  end if
0100
                end if
0101
                if(typitr .gt. 0) then
                  if(typitr .eq. 1) then
0102
0103
                    dfdtht=(rbar22*r22-zone)*dfdtht
0104
                  else
0105
                     dfdtht=(rbar11*r11-zone)*dfdtht
0106
                  end if
0107
                end if
0108
                return
0109
         300
                format('0Iterations:
                                           exact')
0110
         301
                format('OIterations: inexact')
                                                              d real
0111
         302
                format(8x, 'real
                                                f mag
                                                                           d imag',5x,
                                      imag
0112
                        'dfdt real dfdt imag')
         303
0113
                format(5x,2f8.4,1pe12.3,2(1x,2e11.3))
                format('Warning ITERAT: During RPOLY=1, starting fmag (', 1pe10.4,') is smaller than final fmag (',1pe10.4,')')
0114
         304
0115
```

end

```
0001
              subroutine mdhnkl (z,h1,h2,h1prme,h2prme,theta,idbg)
0002
        C
0003
              implicit complex*16 (a-h,o-z)
0004
              complex*16 i,mpower,mterm
0005
              real *8 a,b,c,d,cap,part1,part2,zmag
0006
              character #4 idbg
0007
              dimension a(30), b(30), c(30), d(30), cap(30), part1(2), part2(2)
8000
              equivalence (part1, term4), (part2, sum4)
                           9.3043671692922944819d-01.
                                                         3.1014557230974314911d+01.
0009
                                                         5.7434365242545027449d+02,
0010
                           2.0676371487316209897d+02,
             $
0011
                           8.7021765519007617234d+02.
                                                         8.2877871922864397320d+02,
             $
0012
                           5.4168543740434246542d+02,
                                                         2.5794544638302022111d+02.
             $
0013
                           9.3458495066311674231d+01,
                                                         2.6626351870744066662d+01,
             $
                                                         1.1592803844803233472d+00,
0014
                           6.1210004300561072794d+00,
0015
                           1.8401275944132116616d-01,
                                                         2.4833030963741048003d-02,
0016
                           2.8842080097260218300d-03,
                                                         2.9133414239656786138d-04,
                           2.5827494893312753646d-05,
                                                         2.0256858739853140063d-06.
0017
0018
                           1.4155736366074870734d-07,
                                                         8.8695090013000443124d-09.
             $
0019
                           5.0110220346327933889d-10,
                                                         2.5658074934115685526d-11,
             $
0020
                           1.1961806496091228666d-12,
                                                         5.0988092481207283185d-14,
              $
                                                         7.1886100863126905797d-17,
0021
                           1.9948392989517716388d-15,
0022
                           2.3938095525516785112d-18,
                                                         7.3883010881224645255d-20,
0023
                           2.1194208514407528762d-21,
                                                         5.6653858632471341093d-23/
0024
                           6.7829872514427588456d-01,
                                                         1.1304978752404598033d+01,
0025
                                                         1.1962940478735024376d+02,
                           5.3833232154307609704d+01.
0026
              $
                                                         1.2780919314887846509d+02,
                           1.5337103177865415841d+02,
             $
0027
                           7.4742218215718400631d+01,
                                                         3.2355938621523117060d+01,
             $
0028
                           1.0785312873841039006d+01,
                                                         2.8532573740320209005d+00,
0029
              $
                           6.1360373635097223595d-01,
                                                         1.0937678009821251966d-01,
0030
                           1.6422939954686564465d-02,
                                                         2.1055051223957133911d-03,
0031
              $
                           2.3316778764072130571d-04,
                                                         2.2528288660939256561d-05.
0032
                           1.9156708045016374595d-06,
                                                         1.4446989475879618839d-07.
0033
                           9.7286124416697769730d-09,
                                                         5.8854279743918795891d-10.
0034
                           3.2160808603234314644d-11,
                                                         1.5952782045255116351d-12,
              $
0035
                           7.2151886229105003778d-14.
                                                         2.9876557444763976717d-15.
0036
              $
                           1.1368553061173507104d-16
                                                         3.9889659863766691603d-18.
0037
                           1.2946984700995355913d-19,
                                                         3.8985199340546088228d-21.
0038
                           1.0920223904914870636d-22,
                                                         2.8527230681595795812d-24/
0039
                           4.6521835846461472410d-01,
               data c
                                                         6.2029114461948629822d+00.
0040
                           2.5845464359145262382d+01,
                                                         5.2213059311404570392d+01.
              $
                                                         4.8751689366390821897d+01,
0041
                           6.2158403942148298012d+01,
0042
                                                         1.1215019407957400909d+01,
                           2.7084271870217123228a+01.
                           3.5945575025504490022d+00,
0043
              $
                                                         9.1815006450841609147d-01,
0044
              $
                           .1.9128126343925335199d-01.
                                                         3.3122296699437809740d-02.
              $
0045
                           4.8424410379295043444d-03.
                                                         6.0568368204246458321d-04.
0046
                           6.5550182039227768583d-05.
                                                         6.1985987743950608612d-06.
0047
              $
                           5.1654989786625507119d-07.
                                                         3.8220488188402150986d-08.
0048
                           2.5278100653705126277d-09.
                                                         1.5033066103898380141d-10.
0049
                           8.0822936042464409157d-12.
                                                         3.9473961437101054471d-13.
0050
                           1.7590891906016512675d-14.
                                                         7.1814214762263778920d-16.
0051
                           2.6957287823672589641d-17,
                                                         9.3358572549515461865d-19.
0052
                           2.9922619406895981315d-20.
                                                         8.9015675760511620701d-22,
0053
                           2.4644428505125033375d-23.
                                                         6.3656020935361057409d-25/
0054
               data d
                           6.7829872514427588456d-01.
                                                         4.5219915009618392131d+01.
0055
                           3.7683262508015326776d+02,
                                                         1.1962940478735024344d+03.
0056
                           1.9938234131225040548d+03,
                                                         2.0449470903820554375d+03.
0057
                           1.4201021460986496090d+03.
                                                         7.1183064967350857463d+02,
```

```
MDHNKL
                                                        7.989120647289888551110+61,
0058
                           2.6963282184602597492d+02.
             2
                           1.9021715826880139294d+01,
0059
                                                        3.7188105233392256682d+00,
             $
                                                        8.4220204895828535644d-02.
0060
                           6.0764877832340288572d-01.
             S
0061
                           1.0026214868551016149d-02.
                                                        1.0363012784032058021d-03.
                           9.3867869420580235442d-05.
                                                        7.5124345274574017960d-06.
0062
0063
             S
                           5.3507368429183773360d-07.
                                                        3.4135482251472901638d-08.
             $
                           1.9618093247972931935d-09,
0064
                                                        1.0209780508963274472d-10.
             S
0065
                           4.8341763773500352579d-12,
                                                        2.0913590211334783723d-13,
             S
0066
                           8.2990437346566602039d-15.
                                                        3.0316141496462685641d-16.
             S
                           1.0228117913786331176d-17,
0067
                                                        3.1967863459247792364d-19
                           9.2821903191776400453d-21.
0068
             $
                                                        2.5103962999804300309d-22/
              data cap /
                                                        8.355034722222222116d-02.
0069
                           1.041666666666666663d-01.
0070
                           1.2822657455632716019d-01.
                                                        2.9184902646414046315d-01,
0071
                           8.8162726744375764874d-01.
                                                        3.3214082818627675264d+00.
0072
             S
                           1.4995762986862554546d+01,
                                                        7.8923013011586517530d+01,
             5
0073
                           4.7445153886826431887d+02,
                                                        3.2074900908906619004d+03,
             $
0074
                           2.4086549640874004605d+04.
                                                        1.9892311916950979121d+05
0075
             S
                           1.7919020077753438063d+06.
                                                        1.7484377180034121023d+07,
0076
             $
                           1.8370737967633072978d+08,
                                                        2.0679040329451551508d+09,
0077
             $
                           2.4827519375935888472d+10.
                                                        3.1669454981734887315d+11.
0078
             $
                           4.2771126865134715582d+12,
                                                        6.0971132411392560749d+13.
0079
                           9.1486942234356396792d+14.
                                                        1.4413525170009350101d+16.
0080
             $
                           2.3788844395175757942d+17,
                                                        4.1046081600946921885d+18,
0081
             $
                           7.3900049415704853993d+19,
                                                        1.3859220004603943141d+21,
0082
             $
                           2.7030825930275761623d+22,
                                                        5.4747478619645573335d+23
0083
                           1.1498937014386333524d+25.
                                                        2.5014180692753603969d+26/
0084
              data i/(0.d0,1.d0)/
0085
              data one/(1.d0,0.d0)/, two/(2.d0,0.d0)/, zero/(0.d0,0.d0)/
0086
              data root3/(1.73205080756888d0,0.d0)/
0087
              data alpha/(8.53667218838951d-1,0.d0)/
8800
              data const1/( 2.58819045102522d-01,-9.65925826289067d-01)/
0089
              data const2/( 2.58819045102522d-01, 9.65925826289067d-01)/
              data const3/(-9.65925826289067d-01, 2.58819045102522d-01)/
0090
              data const4/(-9.65925826289067d-01,-2.58819045102522d-01)/
0091
0092
0093
              zpower=one
0094
              sum3=zero
0095
              sum4=zero
0096
              zmag=cdabs(z)
               if(zmag .gt. 6.1d0) go to 70
0097
0098
              sum1=zero
0099
              sum2=zero
0100
              zterm=-z**3/(200.d0,0.d0)
0101
              do 50 m=1,30
0102
              sum1=sum1+dcmplx(a(m),0.d0)*zpower
0103
              sum2=sum2+dcmplx(b(m),0.d0)*zpower
0104
              sum3=sum3+dcmplx(c(m),0.d0)*zpower
0105
              term4=dcmplx(d(m),0.d0)*zpower
0106
              sum4=sum4+term4
0107
              if (dabs(part1(1)) . le. 1.d-17*dabs(part2(1)) . and.
```

dabs(part1(2)) .le. 1.d-17\*dabs(part2(2))) go to 60

0108 0109

0110

0111 0112

0113

0114

50

60

zpower=zpower\*zterm

h1=z\*sum2+gm2f

h2=h1-two+gm2f

h1prme=sum4+gpmfp

gm2f=i\*(z\*sum2-two\*sum1)/root3
gpmfp=i\*(sum4+two\*z\*z\*sum3)/root3

```
MDHNKL
```

```
0115
              h2prme=h1prme-two*gpmfp
0116
              go to 999
        70
0117
              mpower=one
0118
              sum1=one
0119
              sum2=one
0120
              rtz=cdsqrt(z)
0121
              sqrtzb=rtz*z
              zterm=i/sqrtzb
0122
0123
              mterm=-zterm
0124
              dm=zero
0125
              term3=one
              do 80 m=1,30
0126
0127
              zpower=zpower*zterm
0128
              mpower=mpower*mterm
0129
              dm=dm+one
0130
              term1=dcmp/x(cap(m),0.d0)*zpower
              term2=dcmplx(cap(m),0.d0)*mpower
0131
               if (cdabs(term2/term3) .ge. 1.d0) go to 81
0132
0133
              sum1=sum1+term1
              sum2=sum2+term2
0134
              sum3=sum3+dm*term1
0135
0136
              term4=dm*term2
0137
              sum4=sum4+term4
               if(dabs(part1(1)/part2(1))).le. 1.d-17 .and.
0138
0139
                  dabs(part1(2)/part2(2)) .le. 1.d-17) go to 81
0140
        80
              term3=term2
0141
        81
              zterm=(-1.5d0,0.d0)/z
0142
              sum3=sum3*zterm
0143
               sum4=sum4*zterm
0144
               term1=((-0.25d0,0.d0)-i*sqrtzb)/z
0145
               term2=((-0.25d0,0.d0)+i*sqrtzb)/z
0146
               exp1=cdexp((0.d0,0.666666666666666667d0)*sqrtzb)
0147
               exp2=const1*exp1
0148
               exp3=const2/exp1
0149
               exp4=const3*exp1
0150
               exp5=const4/exp1
0151
               zterm=alpha/cdsqrt(rtz)
0152
               term4=z
0153
               if(part1(1) .ge. 0.d0 .or. part1(2) .ge. 0.d0) go to 90
0154
               h1=zterm*(exp2*sum2+exp5*sum1)
0155
               h1prme=zterm*(exp2*(sum2*term2+sum4)+exp5*(sum1*term1+sum3))
0156
               go to 110
0157
        90
               h1=zterm*exp2*sum2
0158
               h1prme=zterm*exp2*(sum2*term2+sum4)
0159
        110
               if(part1(1) .ge. 0.d0 .or. part1(2) .lt. 0.d0) go to 120
0160
               h2=zterm*(exp3*sum1+exp4*sum2)
0161
               h2prme=zterm*(exp3*(sum1*term1+sum3)+exp4*(sum2*term2+sum4))
0162
               go to 999
0163
        120
               h2=zterm*exp3*sum1
0164
               h2prme=zterm*exp3*(sum1*term1+sum3)
0165
               calculate wronskian as partial check on validity
        999
0166
               sum4=h1*h2prme-h1prme*h2
0167
               if(dabs(part2(1)) .le. 1.d-8 .and.
                  dabs(part2(2)+1.457495441040461d0) .le. 1.d-8) go to 1000
0168
0169
               print 1001, sum4, theta, idbg
0170
        1000 return
0171
        1001 format(' ***** possible error in mdhnkl: w = ',1p2e15.6,
```

**MDHNKL** 

```
0001
                subroutine newmag(j,r,phij,thet,bmf,dip,b,br,bp,bt)
0002
        c
0003
        c
                Returns parameters of the geomagnetic field
0004
        C
0005
                         J=0: Use spherical earth
        C
                Input:
                              Use spheroidal earth
0006
        c
                         J=1:
0007
                              is altitude in km
        C
8000
                        PHIJ is West longitude in radians
        C
0009
                        THET is co-latitude in radians
        ¢
0010
        C
0011
                Output:
                         BMF is declination of the geomagnetic field
        C
0012
                         DIP is dip angle
        C
0013
                              is total field
        C
                         В
0014
        c
                         BR
                              is radial component
0015
                          BP
                              is longitudinal component
        C
0016
                              id latitudinal component
        C
0017
0018
              dimension g(10,10), bm(10)
0019
              data g/.0,3.032193e04,2.522093e03,-3.285459e03,-4.170639e03,1.6928
             $19e03,-6.684202e02,-1.900312e03,-2.405232e02,-9.358495e02,-5.75507
0020
0021
             $0e03,2.131549e03,-5.206994e03,6.237642e03,-4.496227e03,-3.650850e0
             $3,-1.241578e03,2.029996e03,-4.463745e02,-3.659410e02,3.495705e03,-
0022
             $1.085898e02,-1.369823e03,-2.514676e03,-1.943789e03,-1.836598e03,-1
0023
0024
             $.313045e02,-1.626874e02,4.917246e02,-8.068787e02,1.220352e03,-4.75
0025
             $3192e02,1.392784e02,-6.836385e02,8.297622e02,1.568303e02,2.302497e
0026
             $03,-1.540896e02,5.700617e02,1.292881e03,-7.922399e02,1.080333e03,-
0027
             $3.941087e01,2.055201e02,-1.853181e02,3.569555e02,-3.656370e01,3.01
             $2583e02,8.903696e01,-6.436587e02,-2.424140e02,-1.041800e03,5.89817
0028
0029
             $9e02,2.310479e02,-5.887414e01,4.001436e01,-1.209943e-02,9.459898e0
0030
             $0,-1.050984e02,-3.745591e02,3.563806e02,-1.545264e03,-6.828717e02,
0031
             $1.681499e02,2.971388e01,6.276772e00,7.309118e01,-3.402882e01,3.871
0032
             $370e01,-1.670375e01,1.915876e03,7.079673e02,1.857451e02,-2.732077e
0033
             $01,-1.705171e02,5.115862e01,1.302727e01,-3.776955e00,-2.940332e01,
0034
             $3.510623e-01,-4.633602e02,6.821298e02,-2.394838e02,4.549622e02,-3.
0035
             $794850e01,-1.617146e02,6.268821e00,1.004341e01,-4.002399e00,-4.152
0036
             $194e00,2.803131e03,-1.698787e03,-4.244406e02,1.998351e02,6.192396e
0037
             $01,-1.668931e02,-9.080082e01,-5.963821e-01,1.524572e00,-9.238670e-
0038
             $01/
              data bm/9.933492e04,9.933492e04,3.746322e04,2.457753e04,1.329481e0
0039
0040
             $4,6.468820e03,3.385349e03,1.616258e03,7.409154e02,3.641040e02/
0041
              data nmax/10/,berr/0.0001/
0042
0043
        50
              p22=abs(sin(thet))
               if(p22 .eq. 0.) p22=1.e-6
0044
0045
              p21=sqrt(1.-p22*p22)
0046
              re=6356.912+p22*p22*(21.3677+.108*p22*p22)
0047
               ar=(re+r)/6371.2
0048
               if (thet .le. 1.570796327e0) go to 70
0049
              p21 = -p21
0050
        70
               if(j .eq. 0) go to 90
0051
               ssq=p22*p22
0052
               ar=ar+(14.288-ssq+(21.3677+.108+ssq))/6371.2
0053
        90
              ar=1./ar
0054
              n=2
        C
0055
               dp22=p21
0056
              convert to east longitude
        c
0057
              phi=phii
```

```
NEWMAG
```

```
0058
               if(phi) 92,96,94
0059
        92
               phi=-phi
0060
              go to 96
        94
              phi=6.2831853e0-phi
0061
0062
        96
               sp2=sin(phi)
0063
              so2=sin(phi)
0064
               cp2=cos(phi)
0065
              dp21=-p22
0066
               aor=ar*ar*ar
0067
              c2=g(2,2)*cp2+g(1,2)*sp2
0068
              br=-(aor+aor)*(g(2,1)*p21+c2*p22)
0069
               bt=aor*(g(2,1)*dp21+c2*dp22)
0070
               bp=aor*(g(1,2)*cp2-g(2,2)*sp2)*p22
0071
               if (nmax . lt. 3) go to 260
0072
               aor=aor*ar
0073
               err=berr*sqrt((bp/p22)**2+br**2+bt**2)
0074
               if (bm(3) *aor .le. err) go to 260
0075
               sp3=(sp2+sp2)*cp2
0076
               cp3=(cp2+sp2)*(cp2-sp2)
0077
               p31=p21*p21-0.3333333333e0
0078
               p32=p21*p22
0079
               p33=p22*p22
0080
               dp31 = -p32 - p32
0081
               dp32=p21+p21-p33
0082
               dp33 = -dp31
               c2=g(3,2)*cp2+g(1,3)*sp2
0083
0084
               c3=g(3,3)*cp3+g(2,3)*sp3
0085
               br=br-3.0*aor*(g(3,1)*p31+c2*p32+c3*p33)
0086
               bt=bt+aor*(g(3,1)*dp31+c2*dp32+c3*dp33)
               bp=bp-aor*((g(3,2)*sp2-g(1,3)*cp2)*p32+2.0*(g(3,3)*sp3-g(2,3)*cp3)
0087
0088
              $*p33)
0089
               n=4
0090
               if (nmax .1t. 4) go to 260
0091
               aor=aor*ar
0092
               if (bm(4) *aor .le. err) go to 260
0093
               sp4=sp2*cp3+cp2*sp3
0094
               cp4=cp2*cp3-sp2*sp3
0095
               p41=p21*p31-0.2666666e0*p21
               dp41=p21*dp31+dp21*p31-0.2666666e0*dp21
0096
0097
               p42=p21*p32-0.2000000e0*p22
0098
               dp42=p21*dp32+dp21*p32-0.20000000e0*dp22
0099
               p43=p21*p33
0100
               dp43=p21*dp33+dp21*p33
0101
               p44=p22*p33
0102
               dp44=3.0*p43
0103
               c2=g(4,2)*cp2+g(1,4)*sp2
0104
               c3=g(4,3)*cp3+g(2,4)*sp3
0105
               c4=g(4,4)*cp4+g(3,4)*sp4
0106
               br=br-4.0*aor*(g(4,1)*p41+c2*p42+c3*p43+c4*p44)
0107
               bt=bt+aor*(g(4,1)*dp41+c2*dp42+c3*dp43+c4*dp44)
0108
               bp=bp-aor*((g(4,2)*sp2-g(1,4)*cp2)*p42+2.0*(g(4,3)*sp3-g(2,4)*cp3)
0109
              $*p43+3.0*(g(4,4)*sp4-g(3,4)*cp4)*p44)
0110
               if (nmax .lt. 5) go to 260
0111
               aor=aor*ar
0112
               if (bm(5) *aor .le. err) go to 260
0113
               sp5=(sp3+sp3)*cp3
0114
               cp5=(cp3+sp3)*(cp3-sp3)
```

```
NEWMAG
```

```
0115
              p51=p21*p41-0.25714285e0*p31
0116
              p52=p21*p42-0.22857142e0*p32
0117
              dp51=p21+dp41+dp21+p41-0.25714285e0+dp31
0118
              dp52=p21*dp42+dp21*p42-0.22857142e0*dp32
0119
              p53=p21*p43-0.14285714e0*p33
0120
              dp53=p21*dp43+dp21*p43-0.14285714e0*dp33
0121
              p54=p21*p44
0122
              dp54=p21*dp44+dp21*p44
0123
              p55=p22*p44
0124
              dp55=4.0*p54
0125
              c2=g(5,2)*cp2+g(1,5)*sp2
0126
              c3=g(5,3)*cp3+g(2,5)*sp3
0127
              c4=g(5,4)*cp4+g(3,5)*sp4
0128
              c5=g(5,5)*cp5+g(4,5)*sp5
0129
              br=br-5.0*aor*(g(5,1)*p51+c2*p52+c3*p53+c4*p54+c5*p55)
0130
              bt=bt+aor*(g(5,1)*dp51+c2*dp52+c3*dp53+c4*dp54+c5*dp55)
0131
              bp=bp-aor*((g(5,2)*sp2-g(1,5)*cp2)*p52+2.0*(g(5,3)*sp3-g(2,5)*cp3)
0132
             $*p53+3.0*(g(5,4)*sp4-g(3,5)*cp4)*p54+4.0*(g(5,5)*sp5-g(4,5)*cp5)*p
0133
             $55)
0134
        С
              n=6
0135
               if(nmax . lt. 6) go to 260
0136
              aor=aor*ar
0137
               if (bm(6) *aor .le. err) go to 260
0138
              sp6=sp2*cp5+cp2*sp5
0139
              cp6=cp2*cp5-sp2*sp5
0140
              p61=p21*p51-0.25396825e0*p41
0141
              dp61=p21*dp51+dp21*p51-0.25396825e0*dp41
0142
              p62=p21*p52-0.23809523e0*p42
0143
              dp62=p21*dp52+dp21*p52-0.23809523e0*dp42
0144
              p63=p21*p53-0.19047619e0*p43
0145
              dp63=p21*dp53+dp21*p53-0.19047619e0*dp43
0146
              p64=p21*p54-0.11111111e0*p44
0147
              dp64=p21*dp54+dp21*p54-0.111111111e0*dp44
0148
               p65=p21*p55
               dp65=p21*dp55+dp21*p55
0149
0150
              p66=p22*p55
0151
               dp66=5.0*p65
0152
               c2=g(6,2)*cp2+g(1,6)*sp2
0153
               c3=g(6,3)*cp3+g(2,6)*sp3
0154
               c4=g(6,4)*cp4+g(3,6)*sp4
0155
               c5=g(6,5)*cp5+g(4,6)*sp5
0156
               c6=g(6,6)*cp6+g(5,6)*sp6
0157
              br=br-6.0*aor*(g(6,1)*p61+c2*p62+c3*p63+c4*p64+c5*p65+c6*p66)
0158
              bt=bt+aor*(q(6,1)*dp61+c2*dp62+c3*dp63+c4*dp64+c5*dp65+c6*dp66)
0159
              bp=bp-aor*((g(6,2)*sp2-g(1,6)*cp2)*p62+2.0*(g(6,3)*sp3-g(2,6)*cp3)
0160
             $*p63+3.0*(g(6,4)*sp4-g(3,6)*cp4)*p64+4.0*(g(6,5)*sp5-g(4,6)*cp5)*p
0161
             $65+5.0*(g(6,6)*sp6-g(5,6)*cp6)*p66)
0162
               if(nmax .lt. 7) go to 260
0163
               aor=aor*ar
               if (bm(7)*aor .le. err) go to 260
0164
0165
              sp7=(sp4+sp4)*cp4
0166
              cp7 = (cp4 + sp4) * (cp4 - sp4)
0167
              p71=p21*p61-0.25252525e0*p51
0168
              dp71=p21+dp61+dp21+p61-0.25252525e0+dp51
0169
              p72=p21*p62-0.24242424e0*p52
0170
              dp72=p21+dp62+dp21+p62-0.24242424e0+dp52
0171
              p73=p21*p63-0.21212121e0*p53
```

```
NEWMAG
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```
0172
              dp73=p21*dp63+dp21*p63-0.21212121e0*dp53
0173
              p74=p21*p64-0.16161616e0*p54
0174
              dp74=p21*dp64+dp21*p64-0.16161616e0*dp54
0175
              p75=p21+p65-0.09090909e0+p55
0176
              dp75=p21+dp65+dp21+p65-0.09090909e0+dp55
0177
              p76=p21+p66
0178
              dp76=p21+dp66+dp21+p66
0179
              p77=p22*p66
0180
              dp77=6.0*p76
0181
              c2=g(7,2)*cp2+g(1,7)*sp2
0182
              c3=g(7,3)*cp3+g(2,7)*sp3
0183
              c4=g(7,4)*cp4+g(3,7)*sp4
0184
              c5=g(7,5)*cp5+g(4,7)*sp5
0185
              c6=g(7,6)*cp6+g(5,7)*sp6
              c7=g(7,7)*cp7+g(6,7)*sp7
0186
0187
              br=br-7.0*aor*(g(7,1)*p71+c2*p72+c3*p73+c4*p74+c5*p75+c6*p76+c7*p7
0188
0189
              bt=bt+aor*(g(7,1)*dp71+c2*dp72+c3*dp73+c4*dp74+c5*dp75+c6*dp76+c7*
0190
             $dp77)
0191
              bp=bp-aor*((g(7,2)*sp2-g(1,7)*cp2)*p72+2.0*(g(7,3)*sp3-g(2,7)*cp3)
0192
             $*p73+3.0*(g(7,4)*sp4-g(3,7)*cp4)*p74+4.0*(g(7,5)*sp5-g(4,7)*cp5)*p
0193
             $75+5.0*(g(7,6)*sp6-g(5,7)*cp6)*p76+6.0*(g(7,7)*sp7-g(6,7)*cp7)*p77
0194
             5)
0195
              n= 8
        c
0196
              if (nmax .1t. 8) go to 260
0197
              aor=aor*ar
0198
              if (bm(8) *aor .le. err) go to 260
0199
              sp8=sp2+cp7+cp2+sp7
0200
              cp8=cp2*cp7-sp2*sp7
0201
              p81=p21*p71-0.25174825e0*p61
0202
              dp81=p21*dp71+dp21*p71-0.25174825e0*dp61
0203
              p82=p21*p72-0.24475524e0*p62
0204
              dp82=p21*dp72+dp21*p72-0.24475524e0*dp62
0205
              p83=p21*p73-0.22377622e0*p63
0206
              dp83=p21*dp73+dp21*p73-0.22377622e0*dp63
0207
              p84=p21+p74-0.18881118e0+p64
0208
              dp84=p21+dp74+dp21+p74-0.18881118e0+dp64
0209
              p85=p21+p75-0.13986013e0+p65
0210
              dp85=p21*dp75+dp21*p75-0.13986013e0*dp65
0211
              p86=p21+p76-0.07692307e0+p66
0212
              dp86=p21+dp76+dp21+p76-0.07692307e0+dp66
0213
              p87 = p21 * p77
0214
              dp87=p21+dp77+dp21+p77
0215
              p88=p22*p77
0216
              dp88=7.0+p87
0217
              c2=g(8,2)*cp2+g(1,8)*sp2
0218
              c3=g(8,3)*cp3+g(2,8)*sp3
0219
              c4=q(8,4)*cp4+q(3,8)*sp4
0220
              c5=g(8,5)*cp5+g(4,8)*sp5
0221
              c6=g(8,6)*cp6+g(5,8)*sp6
0222
              c7=g(8,7)*cp7+g(6,8)*sp7
0223
              c8=q(8,8)*cp8+q(7,8)*sp8
0224
              br=br-8.0*aor*(g(8,1)*p81+c2*p82+c3*p83+c4*p84+c5*p85+c6*p86+c7*p8
0225
             17+c8+p88)
0226
              bt=bt+aor+(g(8,1)+dp81+c2+dp82+c3+dp83+c4+dp84+c5+dp85+c6+dp86+c7+
0227
             $dp87+c8+dp88)
0228
              bp=bp-aor*((g(8,2)*sp2-g(1,8)*cp2)*p82+2.0*(g(8,3)*sp3-g(2,8)*cp3)
```

<u>Ŷĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸĸ</u>

```
NEWMAG
```

```
0229
             $*p83+3.0*(g(8,4)*sp4-g(3,8)*cp4)*p84+4.0*(g(8,5)*sp5-g(4,8)*cp5)*p
0230
             $85+5.0*(g(8,6)*sp6-g(5,8)*cp6)*p86+6.0*(g(8,7)*sp7-g(6,8)*cp7)*p87
0231
             +7.0*(g(8,8)*sp8-g(7,8)*cp8)*p88
0232
              if (nmax .lt. 9) go to 260
0233
              aor=aor+ar
0234
              if (bm(9) *aor .le. err) go to 260
0235
              sp9=(sp5+sp5)*cp5
0236
              cp9=(cp5+sp5)*(cp5-sp5)
0237
              p91=p21*p81-0.25128205e0*p71
0238
              dp91=p21+dp81+dp21+p81-0.25128205e0+dp71
0239
              p92=p21+p82-0.24615384e0+p72
0240
              dp92=p21+dp82+dp21+p82-0.24615384e0+dp72
0241
              p93=p21+p83-0.23076923e0+p73
0242
              dp93=p21+dp83+dp21+p83-0.23076923e0+dp73
0243
              p94=p21*p84-0.20512820e0*p74
0244
              dp94=p21+dp84+dp21+p84-0.20512820e0+dp74
0245
              p95=p21*p85-0.16923076e0*p75
0246
              dp95=p21+dp85+1p21+p85-0.16923076e0+dp75
0247
              p96=p21*p86-0.12307692e0*p76
0248
              dp96=p21+dp86+dp21+p86-0.12307692e0+dp76
0249
              p97=p21*p87-0.06666666e0*p77
0250
              dp97=p21*dp87+dp21*p87-0.0666666e0*dp77
0251
              p98=p21*p88
0252
              dp98=p21*dp88+dp21*p88
0253
              p99=p22*p88
0254
              dp99=8.0*p98
0255
              c2=g(9,2)*cp2+g(1,9)*sp2
0256
              c3=g(9,3)*cp3+g(2,9)*sp3
0257
              c4=g(9,4)*cp4+g(3,9)*sp4
0258
              c5=g(9,5)*cp5+g(4,9)*sp5
0259
              c6=g(9,6)*cp6+g(5,9)*sp6
0260
              c7=g(9,7)*cp7+g(6,9)*sp7
0261
              c8=g(9,8)*cp8+g(7,9)*sp8
0262
              c9=g(9,9)*cp9+g(8,9)*sp9
0263
              br=br-9.0*aor*(g(9,1)*p91+c2*p92+c3*p93+c4*p94+c5*p95+c6*p96+c7*p9
0264
             $7+c8*p98+c9*p99)
0265
              bt=bt+aor*(g(9,1)*dp91+c2*dp92+c3*dp93+c4*dp94+c5*dp95+c6*dp96+c7*)
0266
             $dp97+c8*dp98+c9*dp99)
0267
              bp=bp-aor*((g(9,2)*sp2-g(1,9)*cp2)*p92+2.0*(g(9,3)*sp3-g(2,9)*cp3)
0268
             $*p93+3.0*(g(9,4)*sp4-g(3,9)*cp4)*p94+4.0*(g(9,5)*sp5-g(4,9)*cp5)*p
0269
             95+5.0*(g(9,6)*sp6-g(5,9)*cp6)*p96+6.0*(g(9,7)*sp7-g(6,9)*cp7)*p97
0270
             +7.0*(g(9,8)*sp8-g(7,9)*cp8)*p98+8.0*(g(9,9)*sp9-g(8,9)*cp9)*p99)
0271
        c
              n = 10
0272
              if (nmax .lt. 10) go to 260
0273
              aor=aor*ar
0274
              if (bm(10) * aor . le. err) go to 260
0275
              sp10=sp2+cp9+cp2*sp9
0276
              cp10=cp2*cp9-sp2*sp9
0277
              p101=p21*p91-0.25098039e0*p81
0278
              dp101=p21+dp91+dp21+p91-0.25098039e0+dp81
0279
              p102=p21*p92-0.24705882e0*p82
0280
              dp102=p21+dp92+dp21+p92-0.24705882e0+dp82
2281
              p103=p21*p93-0.23529411e0*p83
0282
              dp103=p21+dp93+dp21+p93-0.23529411e0+dp83
0283
              p104=p21*p94-0.21568627e0*p84
0284
              dp104=p21*dp94+dp21*p94-0.21568627e0*dp84
0285
              p105=p21*p95-0.18823529e0*p85
```

## **NEWMAG**

```
0286
                                                                         dp105=p21*dp95+dp21*p95-0.18823529e0*dp85
  0287
                                                                         p106=p21*p96-0.15294117e0*p86
  0288
                                                                        dp106=p21*dp96+dp21*p96-0.15294117e0*dp86
  0289
                                                                         p107=p21*p97-0.10980392e0*p87
  0290
                                                                         dp107=p21+dp97+dp21+p97-0.10980392e0+dp87
  0291
                                                                         p108=p21*p98-0.05882352e0*p88
  0292
                                                                         dp108=p21*dp98+dp21*p98-0.05882352e0*dp88
  0293
                                                                        p109=p21*p99
  0294
                                                                         dp109=p21*dp99+dp21*p99
  0295
                                                                        p1010=p22*p99
  0296
                                                                        dp1010=9.0*p109
  0297
                                                                        c2=g(10,2)*cp2+g(1,10)*sp2
  0298
                                                                        c3=g(10,3)*cp3+g(2,10)*sp3
  0299
                                                                        c4=g(10,4)*cp4+g(3,10)*sp4
  0300
                                                                        c5=g(10,5)*cp5+g(4,10)*sp5
  0301
                                                                        c6=g(10,6)*cp6+g(5,10)*sp6
 0302
                                                                        c7=g(10,7)*cp7+g(6,10)*sp7
 0303
                                                                        c8=g(10,8)*cp8+g(7,10)*sp8
 0304
                                                                        c9=g(10,9)*cp9+g(8,10)*sp9
 0305
                                                                        c10=g(10,10)*cp10+g(9,10)*sp10
 0306
                                                                        br=br-10.0*aor*(g(10,1)*p101+c2*p102+c3*p103+c4*p104+c5*p105+c6*p1
 0307
                                                                    $06+c7*p107+c8*p108+c9*p109+c10*p1010)
 0308
                                                                        bt=bt+aor*(g(10,1)*dp101+c2*dp102+c3*dp103+c4*dp104+c5*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*dp105+c6*
 0309
                                                                    1106+c7+dp107+c8+dp108+c9+dp109+c10+dp1010)
                                                                        bp=bp-aor*((g(10,2)*sp2-g(1,10)*cp2)*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10))*p102+2.0*(g(10,3)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,10)*sp3-g(2,
 0310
 0311
                                                                    $*cp3)*p103+3.0*(g(10,4)*sp4-g(3,10)*cp4)*p104+4.0*(g(10,5)*sp5-g(4
                                                                    $,10)*cp5)*p105+5.0*(g(10,6)*sp6-g(5,10)*cp6)*p106+6.0*(g(10,7)*sp7
 0312
                                                                  -g(6,10)*cp7)*p107+7.0*(g(10,8)*sp8-g(7,10)*cp8)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+8.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,9)*p108+9.0*(g(10,
 0313
0314
                                                                  $*sp9-g(8,10)*cp9)*p109+9.0*(g(10,10)*sp10-g(9,10)*cp10)*p1010)
                                         260
0315
                                                                        bp=bp/p22*1.e-5
0316
                                                                       bt=bt + 1.e-5
0317
                                                                        br=br + 1.e-5
0318
                                                                        b=sqrt(br*br+bt*bt+bp*bp)
0319
                                                                        bh=sqrt(bt+bt+bp+bp)
0320
                                                                       bmf = 3.141592654e0 - acos(bt/bh)
0321
                                                                        if (bp . lt. O.) bmf=-bmf
0322
                                                                        dip=acos(bh/b)
0323
                                                                        if (br .gt. 0.) dip=-dip
0324
                                                                        return
0325
                                                                       end
```

```
0001
              subroutine profin(lu,type,maxhts,nprint,nrspec,lmax,hlist,alogen)
0002
        C
0003
              Reads ionospheric profiles
        С
0004
              type=1: electron and ion densities
        С
0005
                    2: collision frequencies
        С
0006
0007
               integer type
0008
              character *80 bcd
0009
              dimension hlist(maxhts), alogen(maxhts, 3), en(3)
              if(type .ne. 2) then
0010
0011
                 read(lu,1010) bcd
0012
                 if(nprint .gt. 1) print 1011,bcd
0013
              end if
              do 202 l=1, maxhts+1
0014
0015
               read(lu,1020,end=900) ht,en
               if(ht .lt. 0.) then
0016
0017
                 |max=|-1|
0018
                 return
0019
               end if
               if (l .ne. 1 .and. ht .ge. hlist(l-1)) then
0020
                 print *, 'ERROR PROFIN: Profile heights out of order'
0021
0022
                 go to 999
0023
              end if
0024
               hlist(1)=ht
0025
               if (type .eq. 1 .and. nrspec .eq. 3) en(3)=en(2)-en(1)
0026
                 if(nprint .gt. 1) print 1021,ht,(en(k),k=1,nrspec)
0027
              do 201 k=1,nrspec
0028
        201
               a \log (l,k) = a \log (a \max 1 (e n(k), 1.e-20))
0029
        202
              continue
              print *, 'ERROR PROFIN: Too many heights in profile'
0030
0031
              go to 999
0032
        900
              print *, 'ERROR PROFIN: Profile input not properly terminated'
0033
        999
               lmax=-1
0034
               return
0035
        1010
              format(a80)
0036
        1011
              format(/1x,a80)
0037
        1020
              format(f7.2,4x,3e10.2)
0038
        1021
              format(f8.2,4x,1p3e10.2)
0039
```

```
0001
              subroutine qartic(q,b3,b2,b1,b0,debug,newq)
0002
              implicit réal +8 (a-h,o-z)
              complex*16 b3,b2,b1,b0,q,b3sq,h,i,g,hprime,gprime,sqroot,
0003
0004
                          p1,p2,cbert0,cbert1,cbert2,omega1,omega2,
0005
                          rootp, rootq, rootr, fncton, ctemp, dfdq, dq
0006
              integer debug
              dimension diff(4),q(4)
0007
              data omega1/(-5.d-1, 8.660254038d-1)/
8000
0009
              data omega2/(-5.d-1,-8.660254038d-1)/
0010
              data to 1/1.d-06/, imax/5/
0011
        C
0012
              iagain=0
0013
              if (newq .eq. 1) go to 30
0014
              newq=1
0015
        10
              b3sa=b3**2
0016
              h=b2-b3sa
0017
              i=b0-(4.d0,0.d0)*b3*b1+(3.d0,0.d0)*b2**2
0018
              g=b1+b3+((-3.d0,0.d0)+b2+(2.d0,0.d0)+b3sq)
0019
               hprime=-i/(12.d0,0.d0)
0020
              gprime=-g**2/(4.d0,0.d0)-h*(h**2+(3.d0,0.d0)*hprime)
0021
        C
0022
              sqroot=cdsqrt(gprime**2+(4.d0,0.d0)*hprime**3)
0023
              p1=(-.5d0,0.d0)*(gprime-sqroot)
0024
               p2=(-.5d0,0.d0)*(gprime+sqroot)
0025
              if(cdabs(p1) .lt. cdabs(p2)) p1=p2
0026
              cbert0=cdexp(cdlog(p1)/(3.d0,0.d0))
0027
              cbert1=omega1*cbert0
0028
              cbert2=omega2*cbert0
0029
0030
              rootp=cdsqrt(cbert0-hprime/cbert0-h)
0031
              rootq=cdsqrt(cbert1-hprime/cbert1-h)
0032
              rootr=cdsqrt(cbert2-hprime/cbert2-h)
0033
              if(cdabs(g) . gt. 1.d-30) then
0034
                sign=-rootp*rootq*rootr*(2.d0,0.d0)/g
0035
                 if(sign .lt. 0.d0) rootr=-rootr
0036
              end if
0037
              q(1)=+rootp+rootq+rootr-b3
0038
              q(2)=+rootp-rootq-rootr-b3
0039
              q(3)=-rootp+rootq-rootr-b3
0040
              q(4)=-rootp-rootq+rootr-b3
0041
        30
0042
               if (debug .gt. 2) print 100,b3,b2,b1,b0
0043
              do 60 n=1.4
0044
              do 40 iter=1.imax
0045
              fncton=(((q(n)+(4.d0,0.d0)*b3)*q(n)+(6.d0,0.d0)*b2)*q(n)
0046
                             +(4.d0,0.d0)*b1)*q(n)+b0
0047
              dfdq=(((4.d0,0.d0)*q(n)+(12.d0,0.d0)*b3)*q(n)
0048
                                       +(12.d0,0.d0) +b2) +q(n) +(4.d0,0.d0) +b1
0049
              dq=-fncton/dfdq
0050
              q(n)=q(n)+dq
0051
              testdq=cdabs(dq/q(n))
0052
              if (testdq .le. tol) go to 60
0053
        40
              continue
0054
               if (iagain .eq. 1) then
0055
                fncton=(((q(n)+(4.d0,0.d0)+b3)+q(n)+(6.d0,0.d0)+b2)+q(n)
0056
                               +(4.d0,0.d0)+b1)+q(n)+b0
0057
                print 101, n, q(n), fncton, dq, iagain
```

```
QARTIC
0058
                 stop
0059
               else
0060
                 iagain=1
0061
                 go to 10
0062
               end if
0063
        60
               continue
0064
0065
               1=0
               do 80 m=2,4
0066
               do 80 n=m,4
0067
0068
               if (dimag(q(n)) . gt. 0.d0) go to 80
0069
               |=|+1
               ctemp=q(n)
0070
0071
               q(n)=q(m-1)
0072
               q(m-1) = ctemp
0073
        80
               continue
0074
               if (1 .eq. 2) go to 99
0075
               do 81 n=1,4
0076
               angq=cdang(q(n)) *57.295779513d0
0077
               if(angq .lt. 135.d0) angq=angq+360.d0
0078
        81
               diff(n) = dabs(angq-315.d0)
0079
               do 82 nm=2,4
0080
               do 82 n=nm,4
0081
               if(diff(n) .gt. diff(nm-1)) go to 82
0082
               temp=diff(n)
               diff(n)=diff(nm-1)
0083
               diff(nm-1)=temp
0084
0085
               ctemp=q(n)
0086
               q(n)=q(nm-1)
0087
               q(nm-1)=ctemp
8800
        82
               continue
0089
        С
0090
        99
               return
0091
        100
               format(/' In QARTIC: b''s =',4(1pel3.4,el2.4))
0092
        101
               format(8h q root ,i1,2h =,1p2e13.5,3x,10hfunction =,2e13.5,3x,
0093
                      4hdq = ,2e13.5,3x,8hiagain = ,i1)
0094
```

end

```
0001
               subroutine rbars
0002
               implicit real *8 (a-h,o-z)
0003
        C
0004
               include 'common1.for'
0020
               include 'common2.for'
               include 'common3.for'
0034
0059
        c
0060
               complex+16 ngsq,sqroot,ratio,ikc,exd,exdsq,z1,z2,
0061
                           p0, h10, h20, h1prm0, h2prm0, caph10, caph20,
0062
                           pd, h1d, h2d, h1prmd, h2prmd, caph1d, caph2d,
0063
                           alst, a2nd, a3rd, a4th, a1, a2, a3, a4, f1, f2
0064
               real *8 kvraot, kvratt, ndsq, n0sq
0065
        C
0066
               ngsq=dcmplx(dble(epsr),-dble(sigma)/(omega*8.85434d-12))
0067
               sgroot=cdsgrt(ngsg-ssg)
0068
        С
0069
               if (dimag(theta) .lt. -10.d0 .or. alpha .eq. 0.) go to 20
0070
               if (d .eq. 0.) go to 10
0071
        C
0072
               kvraot=dexp(dlog(wn/alpha)/3.d0)
0073
               kvratt=kvraot**2
0074
               avrkot=1.d0/kvraot
0075
               avrktt=avrkot**2*0.5d0
0076
               n0sq=1.-alpha*h
0077
               ratio=n0sq/ngsq*sqroot
0078
               p0=kvratt*(n0sq-ssq)
               call mdhnkl(p0,h10,h20,h1prm0,h2prm0,theta,'rb 1')
0079
0080
               caph10=h1prm0+avrktt*h10
0081
               caph20=h2prm0+avrktt+h20
0082
               a1st=caph20-zmplxi*ratio*kvraot*h20
0083
               a2nd=caph10-zmpixi*ratio*kvraot*h10
0084
               a3rd=h2prm0-zmplxi*kvraot*sgroot*h20
               a4th=h1prmO-zmplxi*kvraot*sqroot*h10
0085
0086
               ndsq=1.-alpha*(h-d)
0087
               pd=kvratt*(ndsq-ssq)
0088
               call mdhnkl(pd, h1d, h2d, h1prmd, h2prmd, theta, 'rb 2')
0089
               caph1d=h1prmd+avrktt+h1d
0090
               caph2d=h2prmd+avrktt*h2d
0091
               f1=h2d*a2nd-h1d*a1st
0092
               f2=h2d*a4th-h1d*a3rd
0093
               a1=c*ndsq*f1
0094
               a2=zmpixi+avrkot+(caph1d+a1st-caph2d+a2nd)
0095
               a3=zmplxi*avrkot*(h2prmd*a4th-h1prmd*a3rd)
0096
               a4=c*f2
               rbar11=(a1-a2)/(a1+a2)
0097
0098
               rbar22=(a3+a4)/(a4-a3)
               hg=exp(-.5*alpha*d)*(h20*a2nd-h10*a1st)/f1
0099
0100
               norm11=f1*f1
0101
               norm22=f2*f2
0102
               norm12=f1*f2
0103
               return
0104
0105
        10
               rbar11=(ngsq*c-sqroot)/(ngsq*c+sqroot)
               rbar22=(c-sqroot)/(c+sqroot)
0106
0107
               ha=zone
0108
               norm11=(-2.124292958d0, 0.d0)
0109
               norm22=norm11
```

## **RBARS**

```
0110
              norm12=norm11
0111
              return
0112
        С
0113
        C
              flat earth
        20
              ikc=dcmplx(0.d0,-wn)*c
0114
0115
              exd=cdexp(ikc*d)
0116
              exdsq=exd*exd
0117
              z1=(ngsq*c-sqroot)/(ngsq*c+sqroot)
0118
              z2=(c-sqroot)/(c+sqroot)
0119
              rbarl1=z1*exdsq
0120
              rbar22=z2*exdsq
              hg=exd*(zone+z1)/(zone+rbar11)
0121
0122
              norm11=(zone+rbar11)*(zone+rbar11)/exdsq
0123
              norm22=(zone+rbar22)*(zone+rbar22)/exdsq
0124
              norm12=(zone+rbar11)*(zone+rbar22)/exdsq
0125
              return
0126
              end
```

```
0001
                subroutine recvr(tlng,tclt,xtr,rho,rlng,rclt)
0002
        c
0003
        c
                Returns coordinates of a point which is at a specified great
0004
        С
                circle distance and bearing angle from the input point
0005
        c
                        TLNG is longitude of transmitter
0006
                Input:
        С
                         TCLT is co-latitude of transmitter
0007
        С
8000
                         XTR is geographic bearing angle of receiver
        c
0009
        c
                             is great circle distance to the receiver
0010
        С
0011
                Output: RLNG is longitude of receiver
        С
0012
        С
                          RCLT is co-latitude of receiver
0013
        С
                All coordinates, RHO and XTR are in radians
0014
        С
0015
                Sign convention is + for West and North
        c
0016
        c
0017
                data pi/3.14159265e0/,twopi/6.28318531e0/
0018
        c
0019
                reduce(arg) = sign(amin1(abs(arg),1.),arg)
0020
        С
0021
                ctc|t=cos(tc|t)
                stclt=sin(tclt)
0022
0023
                br=xtr
0024
                gcd=rho
0025
0026
                if (abs(br) .lt. twopi) go to 2
0027
                br=amod(br,twopi)
0028
        2
                if (br .ge. 0.) go to 3
0029
                br=br+twopi
0030
        3
                if (gcd .lt. pi) go to 5
0031
                gcd=twopi-gcd
0032
                br=br+pi
0033
                if(br .ge. twopi) br=br-twopi
0034
        5
                 if (br .le. 1.e-6) go to 10
0035
                 if (abs(br-pi) .le. 1.e-6) go to 14
0036
                 if (abs(gcd-pi) .le. 1.e-6) go to 14
0037
                cgcd=cos(gcd)
0038
                sgcd=sin(gcd)
0039
                crc!t=ctc!t*cgcd+stc!t*sgcd*cos(br)
0040
                srcit=sqrt(1.-crcit**2)
0041
                rclt=acos(reduce(crclt))
0042
                delta=acos(reduce((cgcd-ctclt*crclt)/(stclt*srclt)))
0043
                if (br .lt. pi) delta=-delta
0044
                ring=ting+delta
0045
                go to 20
0046
        C
0047
                receiver is due north, south or on opposite longitude
        C
0048
        10
                rclt=tclt-qcd
0049
                 if(rclt .lt. 0.) go to 12
0050
        11
                ring=tl/g
0051
                crclt=cos(rclt)
0052
                srclt=sin(rclt)
0053
                go to 99
0054
        12
                rclt=-rclt
0055
        13
                rlng=tlng+pi
0056
                crclt=cos(rclt)
0057
                srclt=sin(rclt)
```

RECVR		
0058		go to 20
0059	14	rclt=tclt+gcd
0060		if(rclt .lt. pi) go to 11
0061		rclt=twopi-rclt
0062		go to 13
0063	С	
0064	20	if(rlng .gt. pi) go to 21
0065		if(ring .ltpi) go to 22
0066		go`to 99
0067	21	rlng=rlng-twopi
8300		go to 99
0069	22	ring=ring+twopi
0070	С	J J ,
0071	99	return
0072		end

```
0001
               subroutine rplynm
0002
               implicit real +8 (a-h,o-z)
0003
         C
0004
               include 'common2.for'
               include 'common3.for'
0018
0043
         c
0044
               complex+16 lgmtrx(30,4),prod,tlist1,tlist2
0045
               complex. 8 stheta
0046
               real = 4 dst(30)
0047
               integer use(30)
0048
         C
0049
               m= 1
0050
         10
               if (m + e + 30) and t \cdot t \cdot (1, m) \cdot gt \cdot 0) then
0051
                 thetar=tlist(1,m)
0052
                 theta:=t!ist(2,m)
0053
                 c=cdcos(theta+zdtr)
0054
                 CSQ=C+C
0055
                 s=cds:n(theta+zdtr)
0056
                 55Q=5+5
0057
                 call nteg
                 do 12 n=1.4
0058
0059
         12
                 ||gmtrx(m,n)=logrs(n)
0060
                 adjflg=1
0061
                 m=m+1
0062
                 go to 10
0063
               end if
0064
               - max=m-1
0065
               if(:mex le 1) then
0066
                 print . 'ERROR RPLYNM
                                           Insufficient thist'
0067
                 stop
0068
               . | 50
0069
                 jmax=m:nO(:max,nrtist)
0070
                 ad | 1 3=0
0071
                 return
0072
               end of
0073
         C
9074
               entry _spoiy
0075
               D stance from theta to to st angles
0076
               stheta=theta
9077
               do 24 [=] max
0078
               use/ 1/= 1
0079
               dst 1. =sqrt(' rea! (stheta, -t st(1 1)) + + 2+
         24
0080
                              a:mag(stheta)-t: st(2, 1:, \bullet \bullet 2,
0081
               Order to strangles according to distance
         c
0082
               call sortr(dst, max, use | max, 1 / max)
0083
               Use only ortist angles
         c
0064
               do 50 n=1 4
0085
                ogrs (r =0
2086
               dc 45 [1=1 |max
2067
0008
               thistixdempla(dbie(thist(1 - 1) - dbie(thist(2 - 1)))
0069
               prodezone
0090
               dc 44 ,2=1 , mas
2091
                2=use',2,
2092
                11 : ne
                            2: then
2093
                    st2=drmp = 'db eit st') 2 db e(t st)2 2
0094
                 prod=prod='theta-t: st2;/(t sti-t st2;
```

## **RPLYNM**

0095		end if
0096	44	continue
0097	45	<pre>logrs(n)=logrs(n)+prod*lgmtrx(i1,n)</pre>
0098	50	rs(n)=cdexp(logrs(n))
0099		return
0100		end

```
0001
               subroutine savemo
0002
        c
0003
        c
               This routine writes the mode parameters out to the logical unit
0004
        c
               defined by LUNIT7.
0005
        C
               include 'common1.for'
0006
0022
               include 'common2.for'
0036
        C
               write(lunit7,100) rho,freq,azim,codip,magfld,sigma,epsr,hprout
0037
0038
               do 10 m=1, modes
               write(lunit7,101) tp(m),nterm(m),t term(1,m),t term(2,m),
0039
         10
0040
                                    tp(m), nterm(m), t term(3,m), t term(4,m)
0041
               write(lunit7,102)
0042
               return
0043
               format('r',f7.3,' f',f8.4,' a',f8.3,' c',f8.3,' m',e10.3,
' s',1pe10.3,' e',0pf5.1,' t',f5.1)
         100
0044
0045
               format('1',0p2f9.5,i1,1p4e15.8/'2',0p2f9.5,i1,1p4e15.8) format('')
0046
         101
0047
         102
0048
               end
```

```
0001
              subroutine sortr(array,nra,index,nri,ii,jj)
0002
        С
0003
        C
               algorithm 347, r.c. singleton, communications of the acm, v12, n3, mar69
0004
        С
              sorts array into order of increasing value, from index ii to ji
0005
        C
              also orders index simultaneously if nri gt 1
0006
        C
               the only arithmetic operation on array is subtraction
0007
               the user should consider the possibility of integer overflow
        c
8000
               arrays iu(k) and il(k) permit sorting up to 2**(k+1)-1 elements
        C
0009
        C
0010
               dimension array(1), index(1), iu(36), il(36)
               if(jj .gt. nra) print +, 'warning from sortr: jj gt nra'
0011
0012
              m=1
0013
               i = i i
0014
               j=jj
0015
        5
               if(i .ge. j) go to 70
0016
        10
              k=i
0017
               ij=(i+j)/2
0018
               t=array(ij)
0019
               if (nri .le. 1) go to 15
0020
               n=index(ij)
0021
        15
               if (array(i) .le. t) go to 20
0022
               array(ij)=array(i)
0023
               array(i)=t
0024
               t=array(ij)
0025
               if (nri .le. 1) go to 20
0026
               index(ij)=index(i)
0027
               index(i)=n
0028
               n=index(ij)
0029
        20
               ز= ا
0030
               if (array(j) .ge. t) go to 40
0031
              array(ij) zarray(j)
0032
               array(j)=t
0033
               t=array(ij)
0034
               if (nri .le. 1) go to 25
0035
               index(ij)=index(j)
0036
               index(j)=n
0037
               n=index(ij)
0038
        25
               if (array(i) .le. t) go to 40
0039
               array(ij)=array(i)
0040
               array(i)=t
0041
               t=array(ij)
0042
               if (nri .le. 1) go to 40
0043
               index(ij)=index(i)
0044
               index(i)=n
0045
               n=index(ij)
0046
               go to 40
0047
        30
              array(|)=array(k)
0048
               array(k)=tt
0049
               if (nri .le. 1) go to 40
0050
               index(1)=index(k)
0051
               index(k)=nn
0052
        40
               1=1-1
0053
               if(array(I) .gt. t) go to 40
0054
               tt=array(I)
0055
               if (nr: le. 1) go to 50
0056
               nn=index(1)
0057
        50
              k=k+1
```

```
SORTR
0058
               if (array(k) . It. t) go to 50
0059
               if (k .le. 1) go to 30
0060
               if(I-i .le. j-k) go to 60
0061
               il(m)=i
0062
               iu(m)=1
0063
               i=k
0064
               m=m+1
0065
               go to 80
0066
        60
               il (m) = k
0067
               iu(m)=j
0068
               j=1
0069
               m=m+1
0070
               go to 80
0071
        70
               m=m-1
               if (m .eq. 0) return
0072
0073
               i=i1(m)
0074
               j=iu(m)
0075
        80
               if (j-i) .ge. 11) go to 10
0076
               if (i eq. ii) go to 5
0077
               i=i-1
        90
0078
               i=i+1
0079
               if(i .eq. j) go to 70
0080
               t=array(i+1)
0081
               if (nri .le. 1) go to 95
0082
               n=index(i+1)
        95
               if(array(i) .le. t) go to 90
0083
0084
0085
        100
               array(k+1)=array(k)
0086
               if (nri .le. 1) go to 105
0087
               index(k+1)=index(k)
        105
8800
               k=k-1
0089
               if (t . lt. array(k)) go to 100
0090
               array (k+1)=t
               if(nri le 1) go to 90
0091
0092
               index(k+1)=n
0093
               go to 90
```

0094

end

```
0001
              subroutine wvguid
0002
        C
0003
              This routine drives the generation of mode parameters using the
        C
0004
              input elist.
        c
              If RPOLY is 0, then all calculations are made exactly.
0005
        C
0006
              If RPOLY is 2, then all calculations are made approximately using
        C
0007
        C
              the routine RPLYNM.
8000
              If RPOLY is 1, then the initial calculations are approximate to
        c
0009
              refine the initial solutions and the final solutions are obtained
        c
0010
              using the exact formulation.
        c
0011
        c
0012
               include 'common1.for/list'
0013 1 c
0014 1
              common/input/freq.rho,azim,cod . magfld,sigma,epsr,beta,hprime,
0015 1
              common/path/pathid, tlong, tlat, r'ag, rlat, rbear, dmax, drmin, drmax,
0016 1
0017 1
                     year, month, day, gmt, nprint, nprof, npath, igcd, ignd, mdir, lost,
0018 1
             $
                      lunit7, lx
0019
              common/ionosp/htlist(50), Inlist(50,3), hclist(50), cflist(50,3),
      1
0020
      1
                      charge(3), mratio(3), nrspec, lhtmx, lhtmn, lht, mhtmx, mhtmn, mht
0021
      1 c
0022
              character + 80 pathid
      1
0023
      1
              integer year, day
0024
              real+4 freq,rho,azim,codip,magfld,sigma,epsr,beta,hprime,hprout,
      1
0025
                      tlong, tlat, rlong, rlat, rbear, dmax, drmin, drmax, gmt,
0026 1
                      htlist, Inlist, hclist, cflist, charge, mratio
0027 1 c
              include 'common2.for/list'
0028
0029
      1 c
0030
      1
              common/wg in/elist(2,30),tlist(2,30),dtheta(2),lub(2),deigen(2),
0031
             Ì
     1
                      thtinc,ftol,maxitr,alpha,h,d,prec,wr0,atnmax,debug,typitr,
0032 1
             $
                      rpoly, nrtlst
0033 1
              common/wg out/tp(30), tterm(4,30), nterm(30), mode(30), modes, nmds
0034 1 c
0035 1
              complex+8 tp.tterm.dthta
0036 1
               integer debug typitr rpoly
0037
      1
              real+4_elist,tlist,dtheta,lub,deigen,thtinc,ftol,alpha,h,d,prec,
0038
      1
                      wrO,atnmax
0039
      1 c
0040 1
              egu alence (dtheta dthta)
0041
     1 c
0042
               include 'common3 for/list'
0043
      1 c
0044
      1
              common/f fnctn/omega,wn,thetar,thetai,c,s,csq,ssq,f,dfdtht,
0045
      1
                      hg, norm11, norm22, norm12, rbar11, rbar22,
0046
                      nriter, newq, adjflg, isotrp
      1
0047
      1
              common/r matrx/r11,r22,r12,r21,
0048 1
             5
                      logr11, logr22, logr12, logr21,
0049 1
                      d111dh,d122dh,d112dh,d121dh,ht,delh,topht
0050 1
              common/m matrx/mll,ml2,ml3,m21,m22,m23,m31,m32,m33
0051
     1 c
0052
      1
               integer adjflg
0053
      1
              real+8 omega,wr,thetar,theta+,ht,delh,topht,r(8),logr(8),dlrdh(8)
0054
      1
              0055
      1
                          hg_ngrm11_norm22_norm12_rbar11_rbar22_
0056
      1
             8
                          r11 r22 r12 r21 rs(4)
             3
0057 1
```

!ogr11, logr22, logr12, logr21, logrs(4);

```
WVGUID
0058
      1
                           dl11dh.dl22dh.dl12dh.dl21dh.dlrsdh(4),
                           m11,m12,m13,m21,m22,m23,m31,m32,m33,
0059
      1
0060
      1
              $
                           zero/(0.d0,0.d0)/,zone/(1.d0,0.d0)/,
0061
      1
                           zmplxi/(0.d0,1.d0)/,zdtr/(1.745329252d-2,0.d0)/
0062 1 c
0063 1
               equivalence (thetar, theta),
0064
                            (r11,rs),(logr11,logrs),(dl11dh,dlrsdh),
      1
0065
      1
                            (r11,r), (logr11, logr), (dl11dh, dlrdh)
0066
      1 c
0067
0068
               complex+16 theta0, stp, ratio, store1, store2, store3,
0069
                           wterm, ecomp, mik
0070
               complex* 8 eigen(30)
0071
               real+8 cdang, reflht, capk, stpr, stpi
0072
               integer psave
0073
               character + 20 reason, blank
0074
               equivalence (elist, eigen)
0075
               data blank/'
                                                 '/,reflht/70.d0/
0076
0077
               psave=rpoly
0078
               capk=1./(1.-.5*alpha*h)
0079
               omega=6.283185306d3+freq
0080
               wn=2.0958426d-2*freq
0081
               wterm=dcmp1 \times (0.d0, -.5d0 + wn + reflht)
0082
               mik=dcmplx(0.d0,-1.d3+wn)
0083
               debug=nprint
0084
               adiflo=0
0085
               newq=0
0086
               if (magfld .le. 1.e-10) then
0087
                 isotrp=1
8800
               else
0089
                 if (codip eq 90. .and. (azim.eq.90. .or. azim.eq.270.)) then
0090
0091
                 else
0092
                   isotrp=0
0093
                 end if
0094
               end if
0095
               call intemp
0096
               of (rpoly eq 1) call rplynm
0097
               if (nprint gt 0) print 1010
8900
         10
               kn=0
0099
               ms=0
0100
0101
        13
               if (elist(1, index) = eq 0) go to 62
0102
               theta0=eigen(index)
0103
               kn=kn+1
0104
               ms=ms+1
               mn=mode(kn)
0105
0106
               reason=blank
0107
        15
               theta=theta0
0108
               call iterat
0109
               fmag=cdabs(f)
0110
               if(nriter ge maxitr and fmag gt ftol) then
0111
                 write(reason, 2000) fmag
0112
                 go to 50
0113
               end if
               pmag=cdabs(rbarl1*r12/(zone-rbarl1*r11))
0114
```

```
WVGUID
0115
              thtr=thetar
0116
              thti=thetai
0117
               if(thti .ge. 0.) then
0118
                 write(reason, 2001)
0119
                 go to 50
0120
              end if
0121
               if (kn .gt. 1) then
0122
                 do 30 kd=1,kn-1
0123
                 if(abs(thtr-elist(1,kd)) .gt. deigen(1)) go to 30
0124
                 if(abs(thti-elist(2,kd)) .gt. deigen(2)) go to 30
0125
                 write(reason, 2002) kd
0126
                 go to 50
                 continue
0127
        30
0128
               end if
0129
               eigen(kn)=theta
               if (ms .eq. mn) go to 35
0130
        33
               if(rpoly .eq. 0 .and. nprint .gt. 0) print 1003
0131
0132
              ms=ms+1
0133
               go to 33
0134
        35
               if (rpoly .eq. 1) go to 60
0135
        c
0136
               if(nriter .gt. maxitr/2) then
                 print *, 'Warning WVGD: Excessive iterations for this mode:'
0137
0138
                 lost=2
0139
               end if
               s=cdsin(theta*zdtr)
0140
0141
               stp=s*capk
0142
               at = -8.6858896d3 * wn * dimag(stp)
0143
               vc=1.d0/dreal(stp)
0144
               tp(mn)=-zmplxi*cdlog(cdsqrt(zone-stp*stp)+zmplxi*stp)/zdtr
0145
0146
               ratio=cdsqrt(s)/(dfdtht/zdtr)
0147
               storel=(zone+rbar11)**2*(zone-rbar22*r22)*ratio/rbar11
0148
               store2=(zone+rbar11) * (zone+rbar22) *ratio
0149
               store3=(zone+rbar22) **2*(zone-rbar11*r11) *ratio/rbar22
0150
               ecomp=wterm*store1*(s*hg)**2
0151
               wm=20.d0*d\log10(cdabs(ecomp))
0152
               wa=cdang(ecomp)
0153
               if (nprint .gt. 0) print 1011, thetaO, mn, nriter, eigen (kn), fmag,
0154
                                             pmag,at,vc,wm,wa,tp(mn)
0155
        C
0156
               t term(1,mn)=store1/norm11
0157
               t term(2,mn)=store3/norm22
0158
               t term(3,mn)=store2/norm12*r21
0159
               t term(4,mn)=r12/r21
0160
               if(cdabs(zone-r11*rbar11) .ge. cdabs(zone-r22*rbar22)) then
0161
                 nterm(mn)=2
0162
               else
0163
                 nterm(mn)=1
0164
               end if
0165
               go to 60
0166
0167
         50
               if (rpoly eq 1) go to 63
               if (nprint .gt. 0) print 1012, theta0, nriter, theta, fmag, pmag
0168
0169
               if (rho eq. 0 .or. npath eq. 1) then
0170
                 if (rpoly eq 1) go to 63
0171
        C
                 OK to drop a mode at the transmitter
```

```
WVGUID
               if (kn .eq. 30 .or. index .eq. 30) then
0172
                 kn=kn-1
0173
0174
                 go to 62
0175
               end if
0176
               do 53 m=kn,30
0177
       53
               eigen(m)=eigen(m+1)
0178
               eigen(30)=(0.,0.)
               go to 13
0179
0180
             else
0181
               print *,'ERROR WVGD: Lost mode',mn,' because ',reason
0182
0183
               go to 999
0184
             end if
0185
0186
       60
              if (kn .eq. 30 .or. index .eq. 30) go to 62
0187
              index=index+1
0188
              go to 13
0189
        62
              nmds=kn
0190
              eigen (nmds+1)=(0.,0.)
0191
              if (nmds .eq. 0) go to 65
0192
              if (rpoly .ne. 1) go to 999
0193
        63
              rpoly=0
0194
              go to 10
              print +, 'ERROR WVGD: Lost all modes'
0195
        65
0196
              lost=1
0197
        999
0198
              if(nprint .gt. 0) print 1003
0199
             rpoly=psave
0200
             return
0201
0202
        1003 format(' ')
       0203
0204
0205
0206
                    1x, f9.3, 1x, f6.3, 1x, 2f8.3)
0207
        1012 format(1x,2f7.3,4x,i5,2x,2f7.3,2(1x,1pe9.3))
0208
        2000 format('fmag=',1pe8.2)
             format('thetai .gt. 0.')
0209
        2001
0210
        2002 format('it matches mode', i3)
0211
             end
```

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